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> restart :
>
C1
> SolucionGeneral := y(x) · 2 · (1 - y(x)) = (x - _C1) · 2;
      SolucionGeneral := y(x)2 (1 - y(x)) = (x - _C1)2 (1)
> Solucion := isolate(SolucionGeneral, _C1);
      Solucion := _C1 = -√y(x)2 (1 - y(x)) + x (2)
> Ecuacion := diff(Solucion, x);
      Ecuacion := 0 = - 1/2 · (2 y(x) (1 - y(x)) (d/dx y(x)) - y(x)2 (d/dx y(x))) / √y(x)2 (1 - y(x)) + 1 (3)
> EcuacionBuscada := simplify(isolate(rhs(Ecuacion) = 0, diff(y(x), x)));
      EcuacionBuscada := d/dx y(x) = - 2√-y(x)2 (-1 + y(x)) / (y(x) (-2 + 3 y(x))) (4)
> restart
> EcuacionDiferencial := sin(2·x)/y(x) + x + (y(x) - sin(x)·2/y(x)·2) · diff(y(x), x) = 0;
      EcuacionDiferencial := sin(2 x)/y(x) + x + (y(x) - sin(x)2/y(x)2) (d/dx y(x)) = 0 (5)
> with(DEtools) :
> odeadvisor(EcuacionDiferencial);
      [_exact] (6)
> M(x, y) := sin(2·x)/y + x;
      M(x, y) := sin(2 x)/y + x (7)
> N(x, y) := y - sin(x)·2/y·2;
      N(x, y) := y - sin(x)2/y2 (8)
> DMy := diff(M(x, y), y);
      DMy := - sin(2 x)/y2 (9)
> DNx := diff(N(x, y), x);
      DNx := - 2 sin(x) cos(x)/y2 (10)
> comprobacion := simplify(DMy - DNx) = 0;
      comprobacion := 0 = 0 (11)
> restart
> Ecuacion := diff(y(x), x) = 2·x·y(x)/(3·x·2 - y(x)·2);

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$$Ecuacion := \frac{d}{dx} y(x) = \frac{2xy(x)}{3x^2 - y(x)^2} \quad (12)$$

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> with(DEtools) :
> odeadvisor(Ecuacion);
      [[_homogeneous, class A], _rational, _dAlembert] (13)
```

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> intfactor(Ecuacion);
```

$$\frac{-3x^2 + y(x)^2}{y(x)(-x + y(x))(y(x) + x)} \quad (14)$$

COEFICIENTES HOMOGENEOS

```
> EcuacionSeparable := simplify(isolate(eval(subs(y(x) = u(x)·x, Ecuacion)), diff(u(x), x)));
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$$EcuacionSeparable := \frac{d}{dx} u(x) = -\frac{u(x)(-1 + u(x)^2)}{x(-3 + u(x)^2)} \quad (15)$$

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> P(u) := \frac{u(-1 + u^2)}{(-3 + u^2)}
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$$P(u) := \frac{u(-1 + u^2)}{-3 + u^2} \quad (16)$$

```
> R(x) := x;
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$$R(x) := x \quad (17)$$

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> SolucionIntermedia := int(1/P(u), u) + int(1/R(x), x) = CI;
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$$SolucionIntermedia := -\ln(u - 1) - \ln(u + 1) + 3 \ln(u) + \ln(x) = CI \quad (18)$$

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> Solucion := simplify(subs(u = y/x, SolucionIntermedia));
```

$$Solucion := -\ln\left(-\frac{-y+x}{x}\right) - \ln\left(\frac{y+x}{x}\right) + 3 \ln\left(\frac{y}{x}\right) + \ln(x) = CI \quad (19)$$

```
> SolucionGeneral := simplify(exp(lhs(Solucion))) = C10;
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$$SolucionGeneral := -\frac{y^3}{-y^2 + x^2} = C10 \quad (20)$$

FACTOR INTEGRANTE

```
> Ecuacion;
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$$\frac{d}{dx} y(x) = \frac{2xy(x)}{3x^2 - y(x)^2} \quad (21)$$

```
> M(x, y) := -2·x·y;
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$$M(x, y) := -2yx \quad (22)$$

```
> N(x, y) := 3x^2 - y^2;
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$$N(x, y) := 3x^2 - y^2 \quad (23)$$

```
> FacInt := simplify\left(\frac{-3x^2 + y^2}{y(-x + y)(y + x)}\right)
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$$FacInt := \frac{3x^2 - y^2}{y(-y^2 + x^2)} \quad (24)$$

> $MM(x, y) := simplify(FacInt \cdot M(x, y));$

$$MM(x, y) := -\frac{2(3x^2 - y^2)x}{-y^2 + x^2} \quad (25)$$

> $NN(x, y) := simplify(FacInt \cdot N(x, y));$

$$NN(x, y) := \frac{(3x^2 - y^2)^2}{y(-y^2 + x^2)} \quad (26)$$

> $DMM_y := simplify(diff(MM(x, y), y));$

$$DMM_y := -\frac{8yx^3}{(-y^2 + x^2)^2} \quad (27)$$

> $DNN_x := simplify(expand(diff(NN(x, y), x)));$

$$DNN_x := \frac{2x(-18y^2x^2 + 9x^4 + 5y^4)}{y(-y^2 + x^2)^2} \quad (28)$$

> restart :

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