

> restart :

> LaplaceFunction := $\frac{s}{(s \cdot 2 + 4) \cdot 2}$;

$$\text{LaplaceFunction} := \frac{s}{(s^2 + 4)^2} \quad (1)$$

> with(inttrans) :

> OriginalFunction := invlaplace(LaplaceFunction, s, t);

$$\text{OriginalFunction} := \frac{1}{4} t \sin(2 t) \quad (2)$$

> FirstFunction := $\frac{s}{(s \cdot 2 + 4)}$; SecondFunction := $\frac{2}{(s \cdot 2 + 4)}$;

$$\text{FirstFunction} := \frac{s}{s^2 + 4}$$

$$\text{SecondFunction} := \frac{2}{s^2 + 4} \quad (3)$$

> FunctionOne := invlaplace(FirstFunction, s, t);

$$\text{FunctionOne} := \cos(2 t) \quad (4)$$

> FunctionTwo := invlaplace(SecondFunction, s, t);

$$\text{FunctionTwo} := \sin(2 t) \quad (5)$$

> FunctionWeLookFor := $\frac{1}{2} \cdot \text{int}(\cos(2 \cdot \text{tau}) \cdot \sin(2 \cdot t - 2 \cdot \text{tau}), \text{tau} = 0 .. t)$;

$$\text{FunctionWeLookFor} := \frac{1}{4} t \sin(2 t) \quad (6)$$

> AA := array([[2, 3], [1, 4]]);

$$AA := \begin{bmatrix} 2 & 3 \\ 1 & 4 \end{bmatrix} \quad (7)$$

> with(linalg) :

> MatExp := exponential(AA, t);

$$\text{MatExp} := \begin{bmatrix} \frac{3}{4} e^t + \frac{1}{4} e^{5t} & \frac{3}{4} e^{5t} - \frac{3}{4} e^t \\ \frac{1}{4} e^{5t} - \frac{1}{4} e^t & \frac{1}{4} e^t + \frac{3}{4} e^{5t} \end{bmatrix} \quad (8)$$

> Ident := array([[1, 0], [0, 1]]);

$$\text{Ident} := \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \quad (9)$$

> sIminusA := evalm(s·Ident - AA);

$$s\text{IminusA} := \begin{bmatrix} s - 2 & -3 \\ -1 & s - 4 \end{bmatrix} \quad (10)$$

> InvsIminusA := inverse(sIminusA);

$$InvsIminusA := \begin{bmatrix} \frac{s-4}{s^2-6s+5} & \frac{3}{s^2-6s+5} \\ \frac{1}{s^2-6s+5} & \frac{s-2}{s^2-6s+5} \end{bmatrix} \quad (11)$$

> *ExpMat* := map(convert, map(invlaplace, InvsIminusA, s, t), exp);

$$ExpMat := \begin{bmatrix} \frac{3}{4} e^t + \frac{1}{4} e^{5t} & \frac{3}{4} e^{5t} - \frac{3}{4} e^t \\ \frac{1}{4} e^{5t} - \frac{1}{4} e^t & \frac{1}{4} e^t + \frac{3}{4} e^{5t} \end{bmatrix} \quad (12)$$

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