

```

> restart
> Ecuacion := diff(f(x,y),x$2) + diff(f(x,y),x,y) = diff(f(x,y),y$3);
          Ecuacion :=  $\frac{\partial^2}{\partial x^2} f(x,y) + \frac{\partial^2}{\partial y \partial x} f(x,y) = \frac{\partial^3}{\partial y^3} f(x,y)$  (1)
> Solucion := pdsolve(Ecuacion)
Solucion :=  $f(x,y) = _C3 + _C4 (\_C3 + _C1 x + _C2 y) + \frac{\_C1 (\_C3 + _C1 x + _C2 y) (\_C2 + _C1)}{\_C2^3}$  + _C5 e

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> Ecuacion2 := lhs(Ecuacion) = diff(f(x,y),y);
          Ecuacion2 :=  $\frac{\partial^2}{\partial x^2} f(x,y) + \frac{\partial^2}{\partial y \partial x} f(x,y) = \frac{\partial}{\partial y} f(x,y)$  (3)

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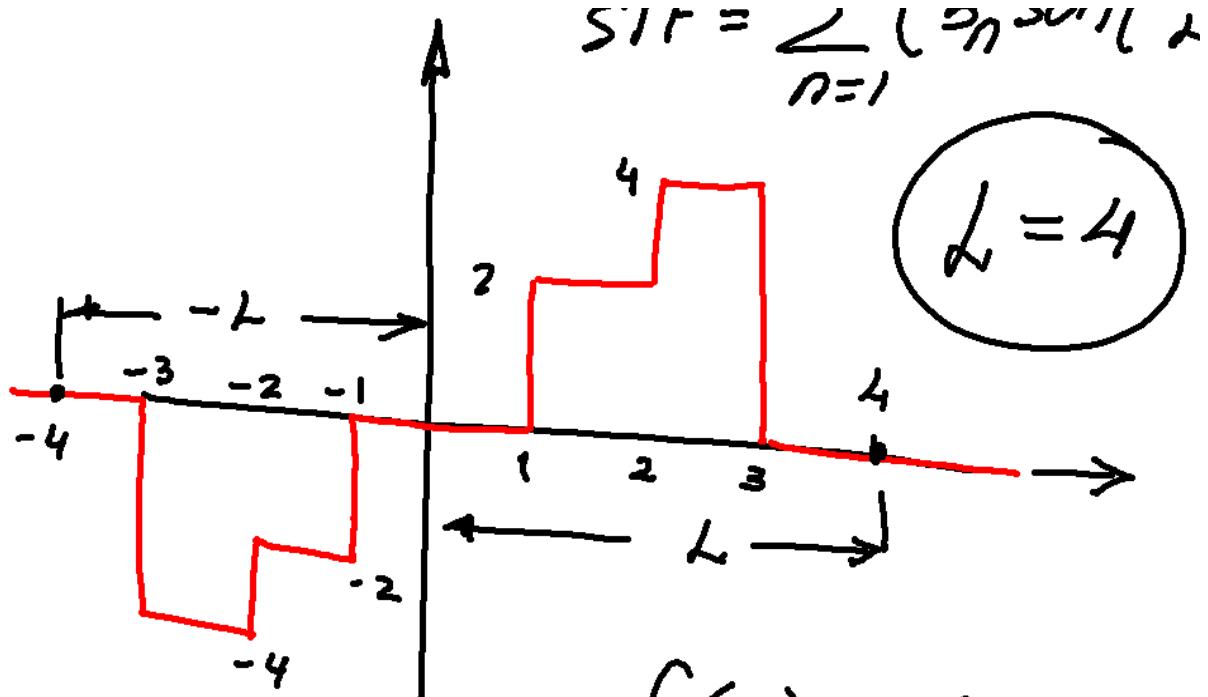
> with(PDEtools) :

> Solucion2 := build(pdsolve(Ecuacion2));

$$Solucion2 := f(x,y) = _C2 _C1 e^{\frac{-c_1 y}{1+c_1}} e^{\frac{-c_1^2 y}{1+c_1}} e^{\frac{-c_1 (x-y)}{1+c_1}}$$
 (4)

> restart

>



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> L := 4;
          L := 4 (5)

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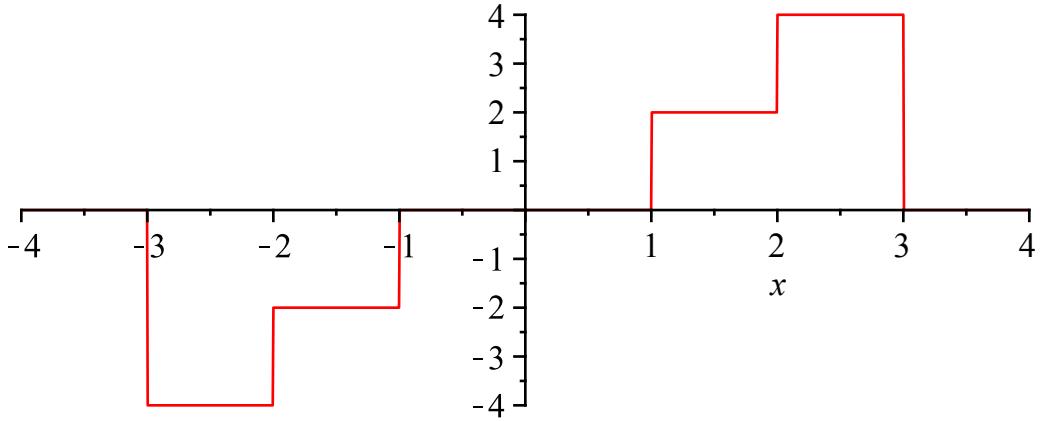
> f(x) := -4·Heaviside(x + 3) + 2·Heaviside(x + 2) + 2·Heaviside(x + 1) + 2·Heaviside(x
      - 1) + 2·Heaviside(x - 2) - 4·Heaviside(x - 3); plot(f(x), x=-L..L);

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f(x) := -4 Heaviside(x + 3) + 2 Heaviside(x + 2) + 2 Heaviside(x + 1) + 2 Heaviside(x
      - 1) + 2 Heaviside(x - 2) - 4 Heaviside(x - 3)

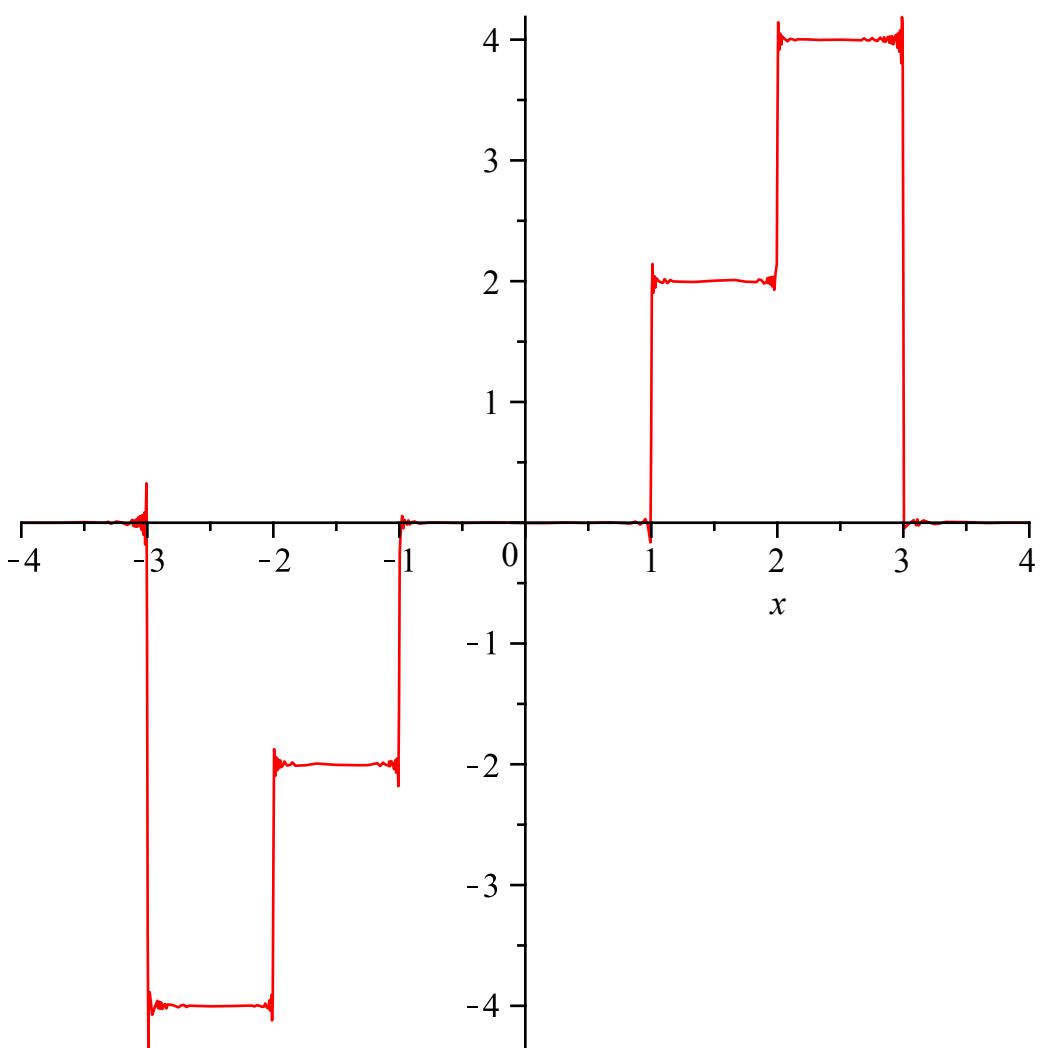
```



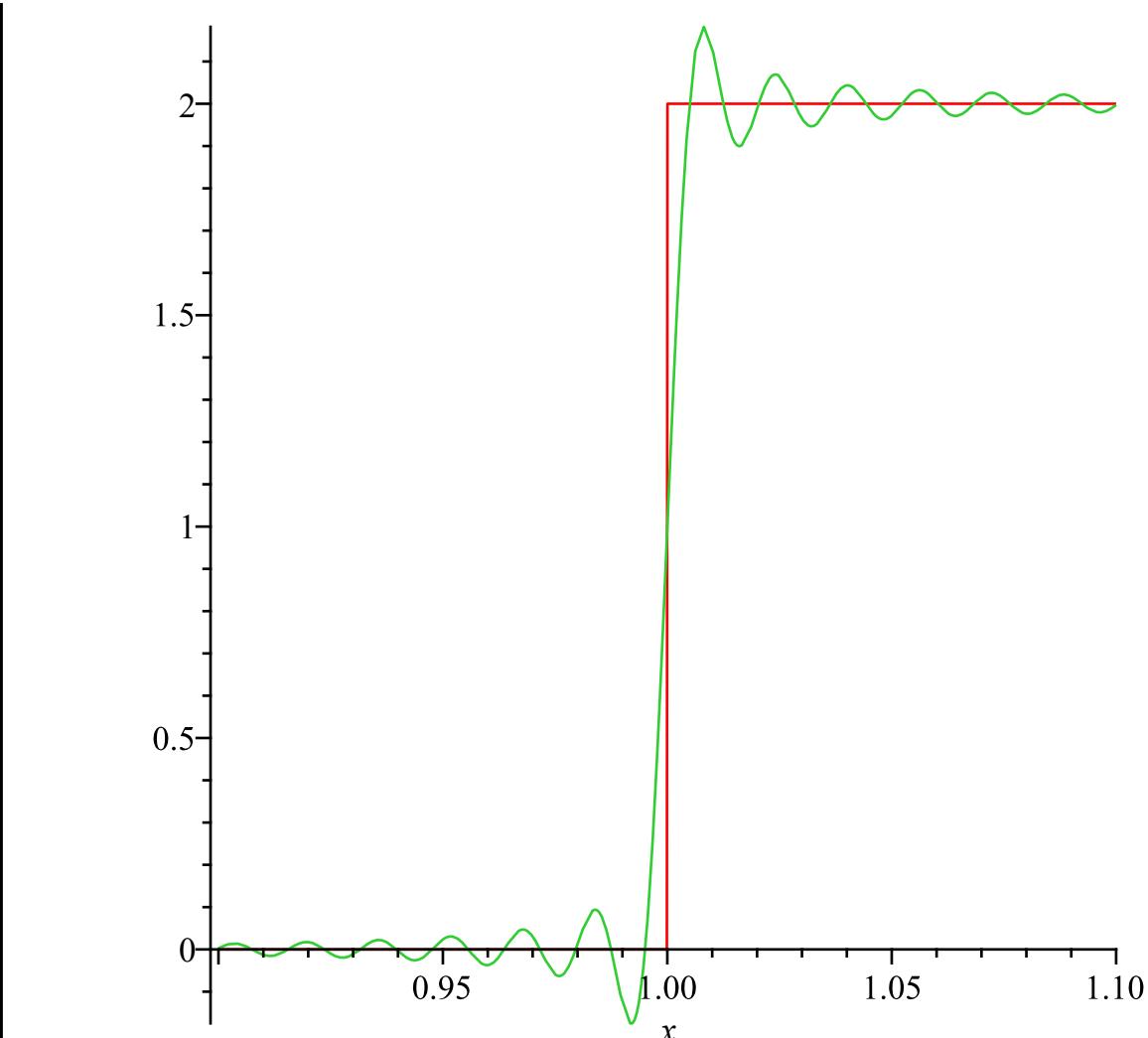
$$\begin{aligned}
 > b_n &:= \left(\frac{1}{L} \right) \cdot \text{int}\left(f(x) \cdot \sin\left(\frac{n \cdot \text{Pi} \cdot x}{L} \right), x = -L .. L \right); \\
 b_n &:= -\frac{8 \cos\left(\frac{3}{4} n \pi\right)}{n \pi} + \frac{4 \cos\left(\frac{1}{2} n \pi\right)}{n \pi} + \frac{4 \cos\left(\frac{1}{4} n \pi\right)}{n \pi}
 \end{aligned} \tag{6}$$

$$\begin{aligned}
 > STF &:= \text{Sum}\left(b_n \cdot \sin\left(\frac{n \cdot \text{Pi} \cdot x}{L} \right), n = 1 .. \text{infinity} \right) \\
 STF &:= \sum_{n=1}^{\infty} \left(-\frac{8 \cos\left(\frac{3}{4} n \pi\right)}{n \pi} + \frac{4 \cos\left(\frac{1}{2} n \pi\right)}{n \pi} + \frac{4 \cos\left(\frac{1}{4} n \pi\right)}{n \pi} \right) \sin\left(\frac{1}{4} n \pi x \right)
 \end{aligned} \tag{7}$$

$$\begin{aligned}
 > STF_{500} &:= \text{sum}\left(b_n \cdot \sin\left(\frac{n \cdot \text{Pi} \cdot x}{L} \right), n = 1 .. 500 \right); \\
 > \text{plot}(STF_{500}, x = -L .. L);
 \end{aligned}$$



```
> plot([f(x), STF500], x=0.9 .. 1.1)
```



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