

> restart

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$$(2y^2 + 3xy + 4x^2y^5) + (2xy + x^2 + 5x^3y^4) \frac{dy}{dx} = 0$$

> Ecuacion := 2·y(x)·2 + 3·x·y(x) + 4·x·2·y(x)·5 + (2·x·y(x) + x·2 + 5·x·3·y(x)·4)·diff(y(x), x) = 0

$$\text{Ecuacion} := 2y(x)^2 + 3xy(x) + 4x^2y(x)^5 + (2xy(x) + x^2 + 5x^3y(x)^4) \left( \frac{d}{dx} y(x) \right) = 0 \quad (1)$$

> with(DEtools) :

> FactorIntegrante := intfactor(Ecuacion)

$$\text{FactorIntegrante} := x \quad (2)$$

> M(x, y) := 2·y·2 + 3·x·y + 4·x·2·y·5

$$M(x, y) := 2y^2 + 3xy + 4x^2y^5 \quad (3)$$

> N(x, y) := 2·x·y + x·2 + 5·x·3·y·4

$$N(x, y) := 2xy + x^2 + 5x^3y^4 \quad (4)$$

> comprobacion<sub>1</sub> := simplify(diff(M(x, y), y) - diff(N(x, y), x)) = 0

$$\text{comprobacion}_1 := 2y + x + 5x^2y^4 = 0 \quad (5)$$

> MM(x, y) := FactorIntegrante·M(x, y); NN(x, y) := FactorIntegrante·N(x, y);

$$MM(x, y) := x(2y^2 + 3xy + 4x^2y^5)$$

$$NN(x, y) := x(2xy + x^2 + 5x^3y^4) \quad (6)$$

> comprobacion<sub>2</sub> := simplify(diff(MM(x, y), y) - diff(NN(x, y), x)) = 0

$$\text{comprobacion}_2 := 0 = 0 \quad (7)$$

> IntMMx := int(MM(x, y), x)

$$\text{IntMMx} := y^5x^4 + yx^3 + y^2x^2 \quad (8)$$

> SolucionGeneral := expand(IntMMx + int((NN(x, y) - diff(IntMMx, y)), y)) = C1

$$\text{SolucionGeneral} := y^5x^4 + yx^3 + y^2x^2 = C1 \quad (9)$$

> restart

> Ecuacion := 2·x·y(x)·2 - 3·y(x)·3 + (7 - 3·x·y(x)·2)·diff(y(x), x) = 0

$$\text{Ecuacion} := 2xy(x)^2 - 3y(x)^3 + (7 - 3xy(x)^2) \left( \frac{d}{dx} y(x) \right) = 0 \quad (10)$$

> with(DEtools) :

> intfactor(Ecuacion)

$$\frac{1}{y(x)^2} \quad (11)$$

> FactInt :=  $\frac{1}{y^2}$ ;

$$\text{FactInt} := \frac{1}{y^2} \quad (12)$$

> M(x, y) := 2·x·y·2 - 3·y·3

$$M(x, y) := 2xy^2 - 3y^3 \quad (13)$$

$$\text{> } N(x, y) := 7 - 3 \cdot x \cdot y \cdot 2$$

$$N(x, y) := 7 - 3xy^2 \quad (14)$$

$$\text{> } \text{comp}_1 := \text{simplify}(\text{diff}(M(x, y), y) - \text{diff}(N(x, y), x)) = 0$$

$$\text{comp}_1 := 4xy - 6y^2 = 0 \quad (15)$$

$$\text{> } MM(x, y) := \text{expand}(\text{FactInt} \cdot M(x, y)); NN(x, y) := \text{expand}(\text{FactInt} \cdot N(x, y))$$

$$MM(x, y) := 2x - 3y$$

$$NN(x, y) := \frac{7}{y^2} - 3x \quad (16)$$

$$\text{> } \text{comp}_2 := \text{simplify}(\text{diff}(MM(x, y), y) - \text{diff}(NN(x, y), x)) = 0$$

$$\text{comp}_2 := 0 = 0 \quad (17)$$

$$\text{> } \text{IntNNy} := \text{int}(NN(x, y), y)$$

$$\text{IntNNy} := -\frac{7}{y} - 3xy \quad (18)$$

$$\text{> } \text{Solucion} := \text{IntNNy} + \text{int}((MM(x, y) - \text{diff}(\text{IntNNy}, x)), x) = C1$$

$$\text{Solucion} := -\frac{7}{y} - 3xy + x^2 = C1 \quad (19)$$

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