

$$M(x, y) + N(x, y) \frac{dy}{dx} = 0$$

$$P(x)Q(y) + R(x)S(y) \frac{dy}{dx} = 0$$

$$\frac{\cancel{P(x)}\cancel{Q(y)}}{\cancel{R(x)}\cancel{Q(y)}} + \frac{\cancel{R(x)}S(y)}{\cancel{R(x)}\cancel{Q(y)}} \frac{dy}{dx} = 0$$

$$\frac{P(x)}{R(x)} + \frac{S(y)}{Q(y)} \frac{dy}{dx} = 0$$

$$\frac{P(x)}{R(x)} dx + \frac{S(y)}{Q(y)} dy = 0$$

Sol. geral $\int \frac{P(x)}{R(x)} dx + \int \frac{S(y)}{Q(y)} dy = C,$

$$\frac{du}{dx} = \frac{\sqrt{1-u^2}}{x}$$

$$P(x) = -\frac{1}{x}$$

$$Q(u) = \sqrt{1-u^2}$$

$$\frac{du}{\sqrt{1-u^2}} = \frac{dx}{x}$$

$$\int P(x) dx + \int \frac{du}{Q(u)} = C_1$$

$$-\frac{dx}{x} + \frac{du}{\sqrt{1-u^2}} = 0$$

$$\text{SG} \rightarrow -\int \frac{dx}{x} + \int \frac{du}{\sqrt{1-u^2}} = C_1$$

$$M(x, y) + N(x, y) \frac{dy}{dx} = 0$$

$$\frac{\partial M}{\partial y} \equiv \frac{\partial N}{\partial x} \quad \text{es exacta}$$

$$S_2 \Rightarrow \int M(x, y) dx + \int \left(N - \frac{\partial}{\partial y} \int M dx \right) dy = C_1$$

