

> restart

> EcuacionDinamica := Masa·diff(s(t), t\$2) = -Hooke·s(t)

$$EcuacionDinamica := Masa \left( \frac{d^2}{dt^2} s(t) \right) = -Hooke s(t) \quad (1)$$

> CondicionesIniciales := s(0) = - (620 - 203) / 1000, D(s)(0) = 0;

$$CondicionesIniciales := s(0) = - \frac{417}{1000}, D(s)(0) = 0 \quad (2)$$

> gravedad := 981 / 100; Masa := (16 / 1000) / gravedad; Hooke := (1914 / 100) / (5 / 10)

$$gravedad := \frac{981}{100}$$

$$Masa := \frac{8}{4905}$$

$$Hooke := \frac{957}{25} \quad (3)$$

> EcuacionDinamica; evalf(%, 3)

$$\frac{8}{4905} \frac{d^2}{dt^2} s(t) = - \frac{957}{25} s(t)$$

$$0.00163 \left( \frac{d^2}{dt^2} s(t) \right) = -38.3 s(t) \quad (4)$$

> Solucion := dsolve({EcuacionDinamica, CondicionesIniciales}); evalf(%, 5)

$$Solucion := s(t) = - \frac{417}{1000} \cos\left(\frac{3}{20} \sqrt{1043130} t\right)$$

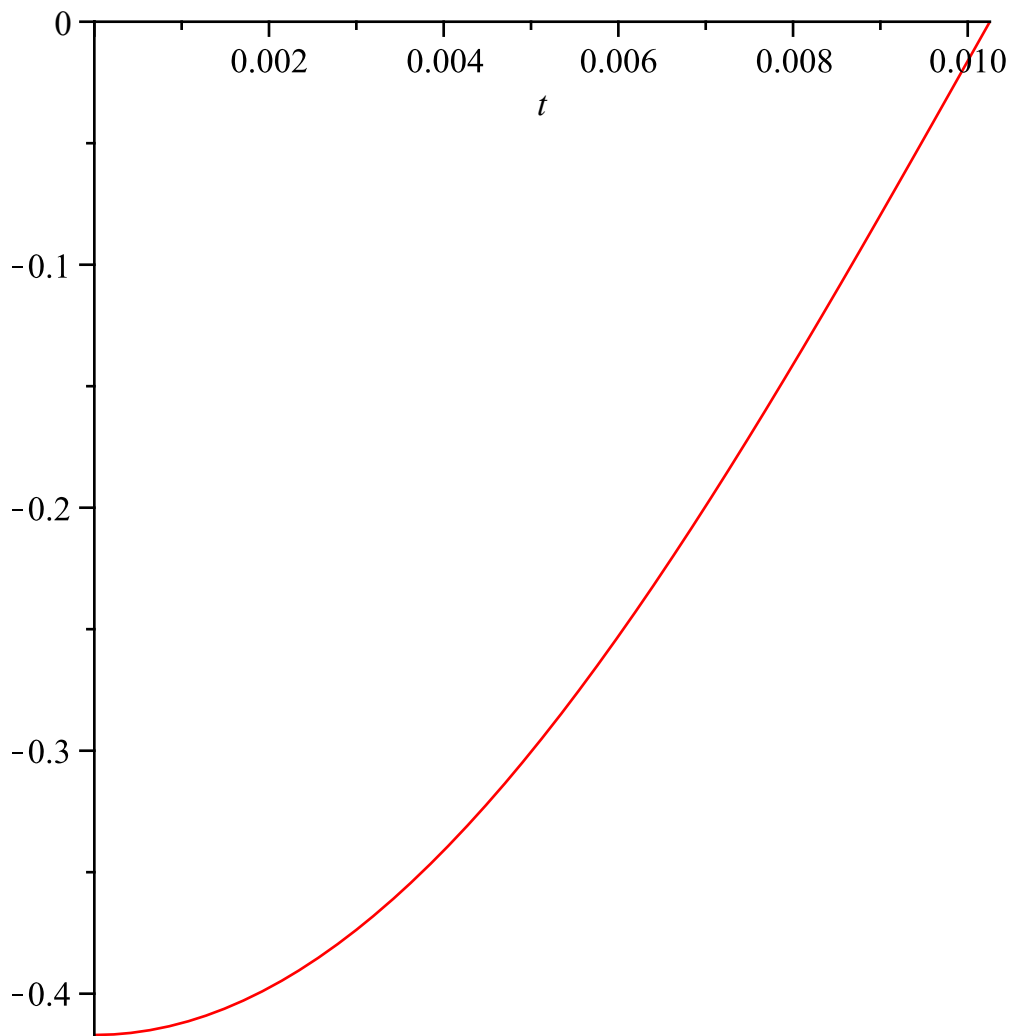
$$s(t) = -0.41700 \cos(153.20 t) \quad (5)$$

> TiempoEscape := solve(rhs(Solucion) = 0, t); evalf(%, 5)

$$TiempoEscape := \frac{1}{312939} \pi \sqrt{1043130}$$

$$0.010253 \quad (6)$$

> plot(rhs(Solucion), t = 0 .. TiempoEscape)




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> *DerSolucion* := diff(*Solucion*, *t*); evalf(%, 5)

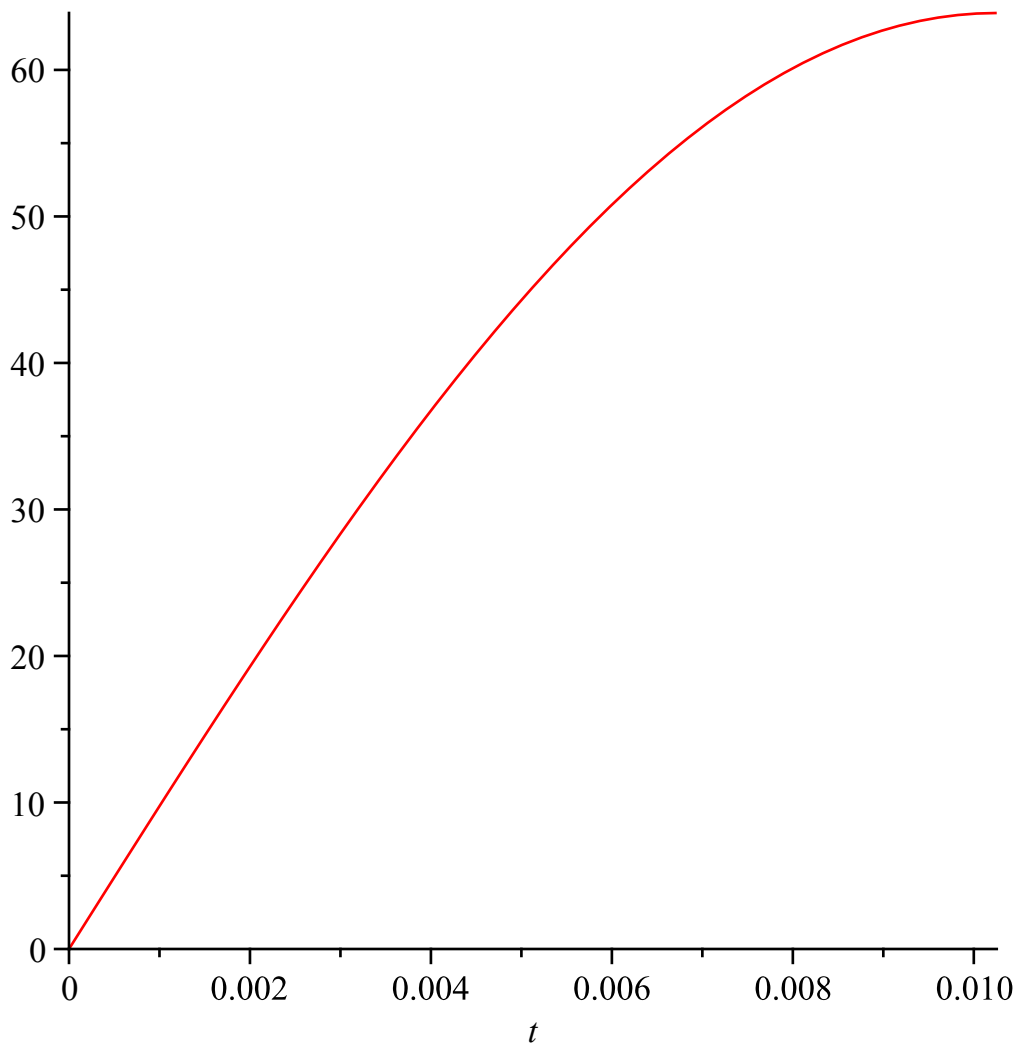
$$DerSolucion := \frac{d}{dt} s(t) = \frac{1251}{20000} \sin\left(\frac{3}{20} \sqrt{1043130} t\right) \sqrt{1043130}$$

$$\frac{d}{dt} s(t) = 63.882 \sin(153.20 t)$$

(7)

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> plot(rhs(*DerSolucion*), t = 0 .. *TiempoEscape*)



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> VelocidadInicial := subs(t = TiempoEscape, rhs(DerSolucion)); evalf(%, 5);
      evalf(%%, 5) * 3600
      -----
      1000
```

$$VelocidadInicial := \frac{1251}{20000} \sin\left(\frac{1}{2} \pi\right) \sqrt{1043130}$$

$$63.882$$

$$229.9752000$$

(8)

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TIRO PARABOLICO

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> EcuacionVertical := diff(y(t), t$2) == -gravedad; evalf(%, 3)
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$$EcuacionVertical := \frac{d^2}{dt^2} y(t) = -\frac{981}{100}$$

$$\frac{d^2}{dt^2} y(t) = -9.81$$

(9)

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> EcuacionHorizontal := diff(x(t), t) = VelocidadInicial * cos\left(\frac{\text{Pi}}{4}\right); evalf(%, 3)
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$$EcuacionHorizontal := \frac{d}{dt} x(t) = \frac{1251}{40000} \sqrt{1043130} \sqrt{2}$$

$$\frac{d}{dt} x(t) = 45.1 \quad (10)$$

$$> \text{CondicionesVerticales} := y(0) = 2, D(y)(0) = \text{VelocidadInicial} \cdot \sin\left(\frac{\text{Pi}}{4}\right); \text{evalf}(\%, 5)$$

$$\text{CondicionesVerticales} := y(0) = 2, D(y)(0) = \frac{1251}{40000} \sqrt{1043130} \sqrt{2}$$

$$y(0) = 2., D(y)(0) = 45.170 \quad (11)$$

$$> \text{CondicionHorizontal} := x(0) = 5$$

$$\text{CondicionHorizontal} := x(0) = 5 \quad (12)$$

$$> \text{SolucionVertical} := \text{dsolve}(\{\text{EcuacionVertical}, \text{CondicionesVerticales}\}); \text{evalf}(\%, 3)$$

$$\text{SolucionVertical} := y(t) = -\frac{981}{200} t^2 + \frac{1251}{40000} \sqrt{1043130} \sqrt{2} t + 2$$

$$y(t) = -4.90 t^2 + 45.1 t + 2. \quad (13)$$

$$> \text{SolucionHorizontal} := \text{dsolve}(\{\text{EcuacionHorizontal}, \text{CondicionHorizontal}\}); \text{evalf}(\%, 5)$$

$$\text{SolucionHorizontal} := x(t) = \frac{1251}{20000} \sqrt{521565} t + 5$$

$$x(t) = 45.173 t + 5. \quad (14)$$

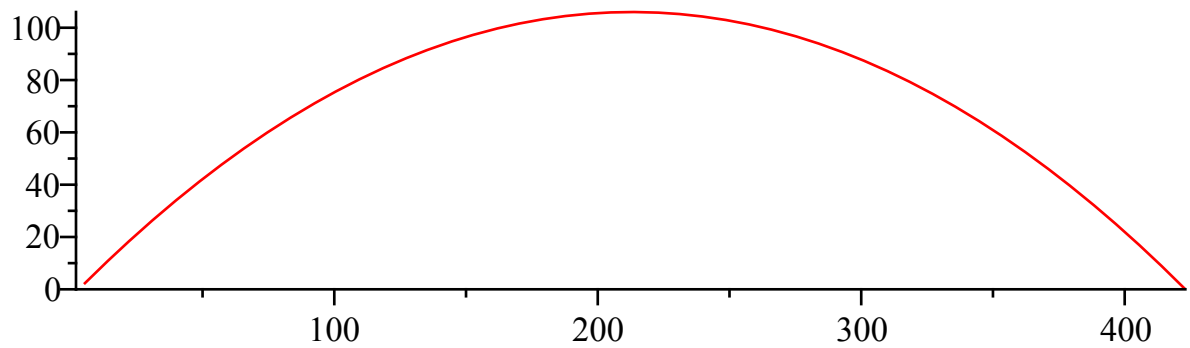
$$> \text{TiempoVuelo} := \text{solve}(\text{rhs}(\text{SolucionVertical}) = 0, t); \text{evalf}(\%, 4)$$

$$\text{TiempoVuelo} := \frac{139}{21800} \sqrt{521565} - \frac{1}{65400} \sqrt{92438416285}, \frac{139}{21800} \sqrt{521565}$$

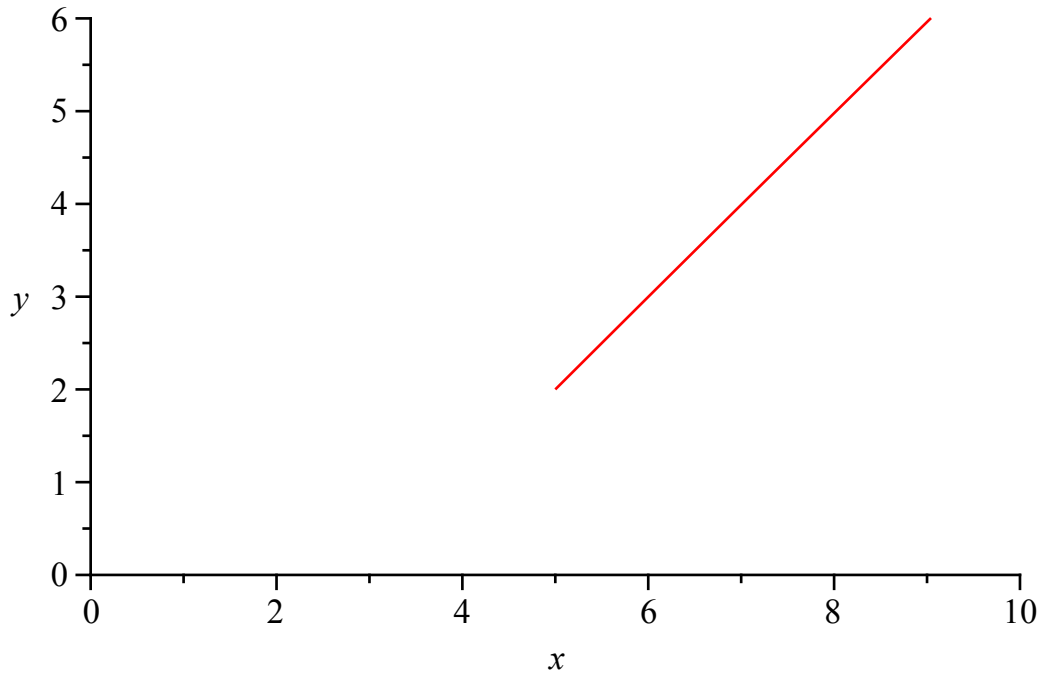
$$+ \frac{1}{65400} \sqrt{92438416285}$$

$$-0.043, 9.253 \quad (15)$$

$$> \text{plot}([ \text{rhs}(\text{SolucionHorizontal}), \text{rhs}(\text{SolucionVertical}), t = 0 .. \text{TiempoVuelo}_2 ], \text{scaling} = \text{CONSTRAINED})$$



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=  
> plot( [rhs(SolucionHorizontal), rhs(SolucionVertical), t = 0 .. 0.1 ], x = 0 .. 10, y = 0 .. 6, scaling  
        = CONSTRAINED)
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> DistanciaHorizontal := subs(t=TiempoVuelo2, rhs(SolucionHorizontal)); evalf(%, 4)
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$$DistanciaHorizontal := \frac{1251}{20000} \sqrt{521565} \left( \frac{139}{21800} \sqrt{521565} + \frac{1}{65400} \sqrt{92438416285} \right) + 5$$

423.0

(16)

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> DerSol := rhs(diff(SolucionVertical, t)) = 0; evalf(%, 3)
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$$DerSol := -\frac{981}{100} t + \frac{1251}{40000} \sqrt{1043130} \sqrt{2} = 0$$

$$-9.81 t + 45.1 = 0.$$

(17)

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> TiempoAlturaMaxima := solve(DerSol, t); evalf(%, 4)
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$$TiempoAlturaMaxima := \frac{139}{43600} \sqrt{1043130} \sqrt{2}$$

4.603

(18)

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> AlturaMaxima := subs(t=TiempoAlturaMaxima, rhs(SolucionVertical)); evalf(%, 4)
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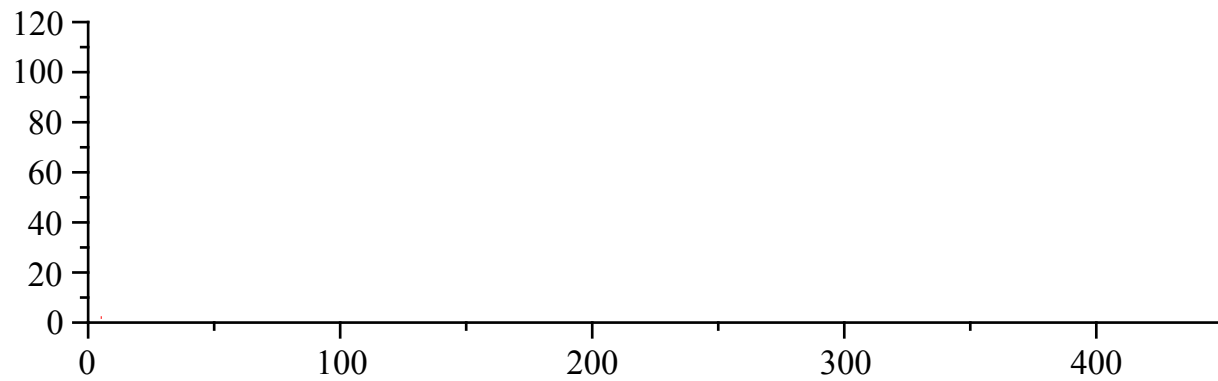
$$AlturaMaxima := \frac{169611773}{1600000}$$

106.0

(19)

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> with(plots) :  
> animatecurve([rhs(SolucionHorizontal), rhs(SolucionVertical), t = 0 ..TiempoVuelo2], view  
= [0 ..450, 0 ..120], scaling = CONSTRAINED, frames = 100)
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