

$$\frac{d^4}{dt^4} y(t) - 5 \left(\frac{d^2}{dt^2} y(t) \right) + 4 y(t) = 5 e^{-2t} \cos(3t)$$

$$y(0) = 5$$

$$D(y)(0) = -4$$

$$D^{(2)}(y)(0) = 3$$

$$D^{(3)}(y)(0) = -2$$

$$\bar{X}(0) = \begin{bmatrix} 5 \\ -4 \\ 3 \\ -2 \end{bmatrix}$$

$$y(t) \Rightarrow y_1(t)$$

$$\frac{dy}{dt} \Rightarrow \frac{d}{dt} y_1(t) = y_2(t)$$

$$\frac{d^2 y}{dt^2} \Rightarrow \frac{dy_2(t)}{dt} = y_3(t)$$

$$\frac{d^3 y}{dt^3} \Rightarrow \frac{dy_3(t)}{dt} = y_4(t)$$

$$\frac{d^4 y}{dt^4} \Rightarrow \frac{dy_4(t)}{dt}$$

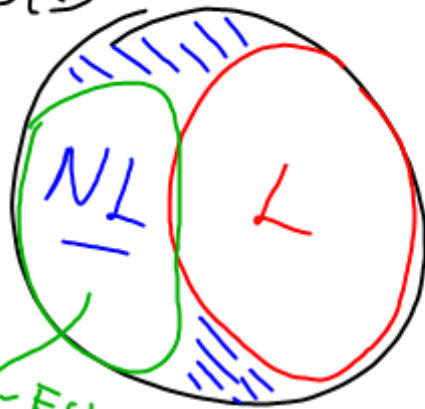
$$\frac{d}{dt} \begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ -4 & 0 & 5 & 0 \end{bmatrix} \begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 0 \\ 5 e^{-2t} \cos(3t) \end{bmatrix}$$

Cap. 1: Ecuaciones No Lineales 1^{er} orden

$$F\left(x, y(x), \frac{dy(x)}{dx}\right) = 0$$

$$\frac{dy}{dx} + p(x)y = q(x)$$

EDO(1)



NL-Esp.

$$\frac{dy}{dx} + p(x)y = 0$$

$$\frac{dy}{dx} = F(x, y)$$

$$\frac{dy}{dx} = F(x, y)$$

$$\frac{dy}{dx} = -\frac{M(x, y)}{N(x, y)}$$

$$N(x, y) \frac{dy}{dx} = -M(x, y)$$

↓

$$M(x, y) + N(x, y) \frac{dy}{dx} = 0$$

4 Métodos de Solución

93. $(xy^2 - y^2 + x - 1) dx + (x^2y - 2xy + x^2 + 2y - 2x + 2) dy = 0$

$$\underbrace{(xy^2 - y^2 + x - 1)}_{M(x,y)} + \underbrace{(x^2y - 2xy + x^2 + 2y - 2x + 2)}_{N(x,y)} \frac{dy}{dx} = 0$$

$$P(x)Q(y) + R(x)S(y) \frac{dy}{dx} = 0$$

$$\frac{\cancel{P(x)}Q(y)}{\cancel{R(x)}Q(y)} + \frac{\cancel{R(x)}S(y)}{\cancel{R(x)}Q(y)} \frac{dy}{dx} = 0$$

$$\frac{P(x)}{R(x)} + \frac{S(y)}{Q(y)} \frac{dy}{dx} = 0$$

$$\frac{S(y)}{Q(y)} \frac{dy}{dx} = -\frac{P(x)}{R(x)}$$

$$\frac{S(y)}{Q(y)} dy = -\frac{P(x)}{R(x)} dx$$

$$\left[\int \frac{S(y)}{Q(y)} dy \right] + k_1 = \left[-\int \frac{P(x)}{R(x)} dx \right] + k_2$$

$$SG \quad \boxed{\left[+ \int \frac{P(x)}{R(x)} dx \right] + \left[\int \frac{S(y)}{Q(y)} dy \right] = C_1}$$

$$\boxed{f(x,y) = C_1} \quad \begin{array}{l} SG - EDO(1) NL \\ \downarrow \\ y(0) = 5 \end{array}$$