

$$F(x, y, y', y'', \dots, y^{(n)}) = 0$$

$$\text{EDO}(1) \quad F(x, y, y') = 0 \quad \begin{cases} L. \\ NL. \end{cases}$$

$$y' \rightarrow p(x) \quad y = q(x)$$

NL

$$y' = f(x, y)$$

$$y' = f(x, y)$$

FORMA GENERAL EDO(1)NL

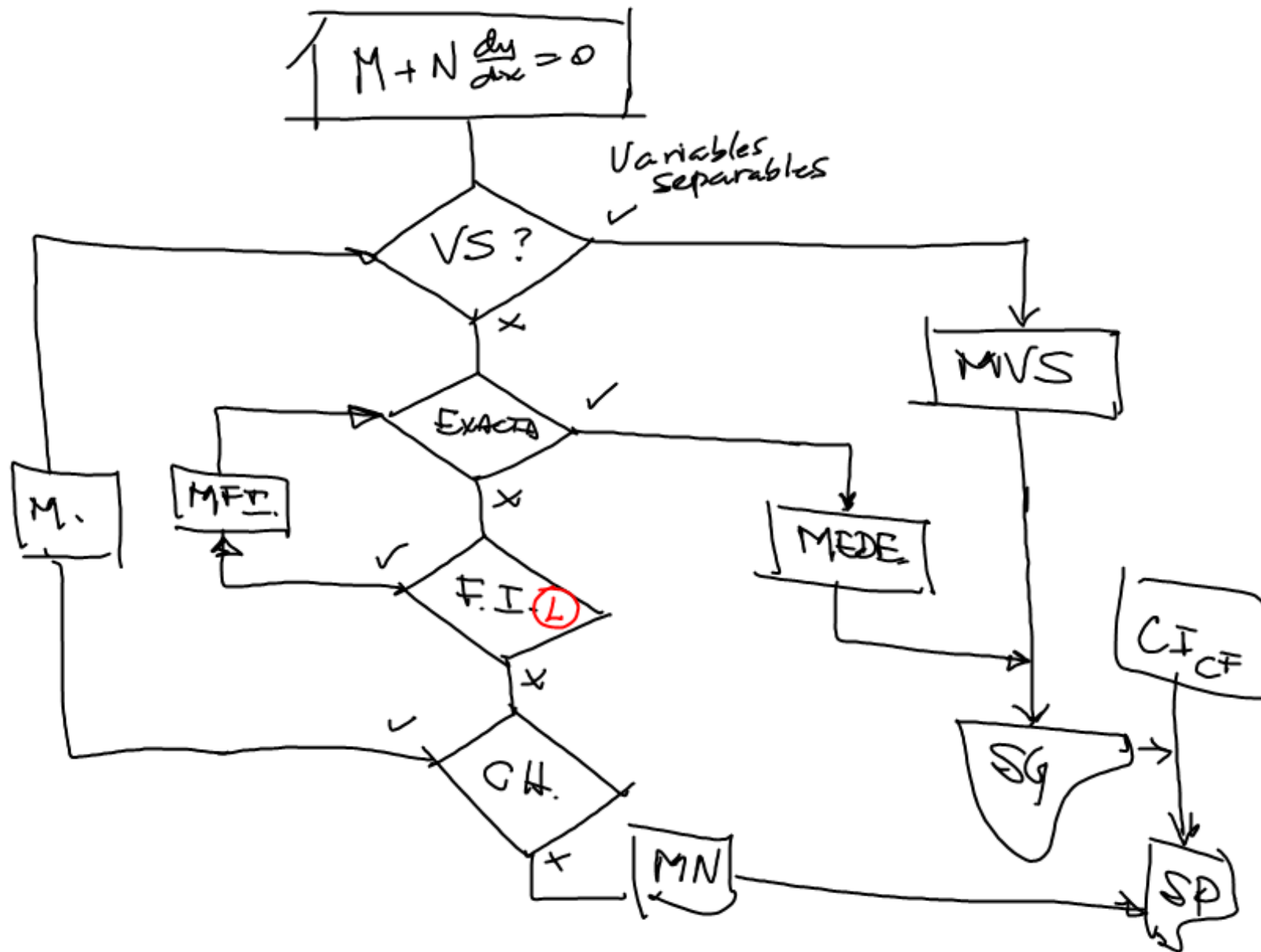
$$\frac{dy}{dx} = - \frac{M(x, y)}{N(x, y)}$$

$$N(x, y) dy = - M(x, y) dx$$

$$M(x, y) dx + N(x, y) dy = 0$$

$$M(x, y) + N(x, y) \frac{dy}{dx} = 0$$

para Maple.



# Método de Variables Separables.

$$M(x, y) + N(x, y) \frac{dy}{dx} = 0$$

$$\downarrow \qquad \qquad \downarrow$$

$$P(x) \cdot Q(y) + R(x) \cdot S(y) \frac{dy}{dx} = 0$$

$$\left( \frac{P(x) \cdot \cancel{Q(y)}}{\cancel{P(x) \cdot Q(y)}} + \frac{\cancel{R(x)} \cdot S(y)}{\cancel{P(x) \cdot Q(y)}} \frac{dy}{dx} = 0 \right.$$

$$\frac{P(x)}{R(x)} + \frac{S(y)}{Q(y)} \frac{dy}{dx} = 0$$

EDO(1) NL

$$\frac{P(x)}{R(x)} dx + \frac{S(y)}{Q(y)} dy = 0$$

SG

$$\int \frac{P(x)}{R(x)} dx + \int \frac{S(y)}{Q(y)} dy = C,$$

$$\boxed{F(x, y) = C}$$

$$(y^2 + xy^2) \frac{dy}{dx} + (x^2 - yx^2) = 0$$

$$(x^2 - yx^2) + (y^2 + xy^2) \frac{dy}{dx} = 0$$

$$x^2(1-y) + (1+x)y^2 \frac{dy}{dx} = 0$$

$$P(x) \Rightarrow x^2 \quad Q(y) \Rightarrow (1-y) \quad R(x) \Rightarrow (1+x) \quad S(y) \Rightarrow y^2$$

$$S_1 \Rightarrow \int \frac{x^2}{x+1} dx + \int \frac{y^2}{1-y} dy = C_1$$

$$\int \frac{x^2}{x+1} dx = \int x dx - \int dx + \int \frac{dx}{x+1}$$

$$\frac{x^2}{x+1} = \frac{x^2 - x + x}{x+1} = \frac{x^2 - x}{x+1} + \frac{x}{x+1}$$

$$\frac{-x}{x+1} = \frac{-x-1+1}{x+1} = -1 + \frac{1}{x+1}$$

$$\int \frac{y^2}{1-y} dy = - \int y dy - \int dy + \int \frac{dy}{1-y}$$

$$= -\frac{y^2}{2} - y - \ln(1-y)$$

$$\frac{y^2}{1-y} = \frac{y^2 - y + y}{1-y} = \frac{y^2 - y}{1-y} + \frac{y}{1-y}$$

$$\frac{y}{1-y} = \frac{y-1+1}{1-y} = -1 + \frac{1}{1-y}$$

$$S_2 \Rightarrow \frac{x^2}{2} - x + \ln(x+1) - \frac{y^2}{2} - y - \ln(1-y) = C_1$$