

> restart

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$$x \ln x \frac{dy}{dx} - y = x^3 (3 \ln x - 1)$$

> Ecuacion := x·log(x)·diff(y(x), x) - y(x) = x·3·(3·log(x) - 1)

$$Ecuacion := x \ln(x) \left(\frac{d}{dx} y(x) \right) - y(x) = x^3 (3 \ln(x) - 1) \quad (1)$$

> EcuacionNormalizada := expand($\frac{lhs(Ecuacion)}{x \cdot \log(x)}$) = expand($\frac{rhs(Ecuacion)}{x \cdot \log(x)}$)

$$EcuacionNormalizada := \frac{d}{dx} y(x) - \frac{y(x)}{x \ln(x)} = 3x^2 - \frac{x^2}{\ln(x)} \quad (2)$$

> p := - $\frac{1}{x \ln(x)}$; q := rhs(EcuacionNormalizada)

$$p := -\frac{1}{x \ln(x)}$$

$$q := 3x^2 - \frac{x^2}{\ln(x)} \quad (3)$$

> IntPosP := int(p, x)

$$IntPosP := -\ln(\ln(x)) \quad (4)$$

> IntNegP := -int(p, x)

$$IntNegP := \ln(\ln(x)) \quad (5)$$

> ExpNeg := exp(IntNegP); ExpPos := exp(IntPosP)

$$ExpNeg := \ln(x)$$

$$ExpPos := \frac{1}{\ln(x)} \quad (6)$$

> ExpPosQ := expand(ExpPos·q)

$$ExpPosQ := \frac{3x^2}{\ln(x)} - \frac{x^2}{\ln(x)^2} \quad (7)$$

> IntQ := int(ExpPosQ, x)

$$IntQ := \frac{x^3}{\ln(x)} \quad (8)$$

> SolucionGeneral := y(x) = C₁·ExpNeg + ExpNeg·IntQ

$$SolucionGeneral := y(x) = C_1 \ln(x) + x^3 \quad (9)$$

> Comporbacion₁ := dsolve(Ecuacion)

$$Comporbacion_1 := y(x) = x^3 + \ln(x) _C1 \quad (10)$$

> Comprobacion₂ := simplify(eval(subs(y(x) = rhs(SolucionGeneral), lhs(Ecuacion) - rhs(Ecuacion) = 0)))

$$\text{Comprobacion}_2 := 0 = 0 \quad (11)$$

> restart

> Ecuacion := y'' - 6 y' + 8 y = 0

$$\text{Ecuacion} := \frac{d^2}{dx^2} y(x) - 6 \left(\frac{d}{dx} y(x) \right) + 8 y(x) = 0 \quad (12)$$

> EcuacionCaracteristica := m · 2 - 6 · m + 8 = 0

$$\text{EcuacionCaracteristica} := m^2 - 6 m + 8 = 0 \quad (13)$$

> Raiz := solve(EcuacionCaracteristica)

$$\text{Raiz} := 4, 2 \quad (14)$$

> SolUno := y(x) = exp(Raiz₁ · x); SolDos := y(x) = exp(Raiz₂ · x)

$$\text{SolUno} := y(x) = e^{4x}$$

$$\text{SolDos} := y(x) = e^{2x} \quad (15)$$

> SolucionGeneral := y(x) = C₁ · rhs(SolUno) + C₂ · rhs(SolDos)

$$\text{SolucionGeneral} := y(x) = C_1 e^{4x} + C_2 e^{2x} \quad (16)$$

> Comprobacion := simplify(eval(subs(y(x) = rhs(SolucionGeneral), Ecuacion)))

$$\text{Comprobacion} := 0 = 0 \quad (17)$$

> Comprobacion₂ := dsolve(Ecuacion)

$$\text{Comprobacion}_2 := y(x) = _C1 e^{4x} + _C2 e^{2x} \quad (18)$$

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