



$$\frac{dV}{dt} = -k V^2$$

$$t_r = ?$$

$$s(0) = 0$$

$$s(t_f) = 0.10 \text{ [m]}$$

$$s'(0) = V(0) = 200 \left[\frac{\text{m}}{\text{s}} \right]$$

$$s'(t_f) = V(t_f) \Rightarrow 80 \left[\frac{\text{m}}{\text{s}} \right]$$

$$\frac{dV}{dt} + kV^2 = 0$$

$$M = kV^2 \quad N = 1$$

MVS

$$P = k \quad Q = V^2 \quad R = 1 \quad S = 1$$

$$\frac{dV}{V^2} + k dt = 0$$

Sg

$$\int \frac{dV}{V^2} + k \int dt = C_1$$

$$\int V^{-2} dV + kt = C_1$$

$$\frac{V^{-1}}{-1} + kt = C_1$$

$$-\frac{1}{V} = C_1 - kt$$

$$\boxed{V = \frac{1}{kt - C_1}}$$

SOLUCIÓN
GENERAL.

$$V(t) = \frac{1}{kt - C_1}$$

$$V(0) \Rightarrow 200 = \frac{1}{k(0) - C_1}$$

$$\Rightarrow 200 = \frac{1}{-C_1}$$

$$-C_1 = \frac{1}{200}$$

$$C_1 = -\frac{1}{200}$$

$$V(t) = \frac{1}{kt + \frac{1}{200}}$$

→

MUS

~~EDO(1)~~ NL

$$\frac{dS(t)}{dt} = \frac{1}{kt + \left(\frac{1}{200}\right)}$$

$$\frac{ds}{dt} = \frac{1}{kt + (\frac{1}{200})}$$

s

$$ds - \frac{dt}{kt + (\frac{1}{200})} = 0$$

$$\int ds - \frac{1}{k} \int \frac{k dt}{kt + (\frac{1}{200})} = C_2$$

(Sg)

$$s - \frac{1}{k} \ln\left(kt + \frac{1}{200}\right) = C_2$$

$$s(0) = 0$$

$$0 - \frac{1}{k} \ln\left(k(0) + \frac{1}{200}\right) = C_2$$

$$-\ln\left(\frac{1}{200}\right) = k C_2$$

$$\frac{\ln(200)}{k} = C_2$$

$$s(t) = 0.5784 + \frac{1}{9.16} \ln\left(9.16t + 0.005\right)$$

(Sp)

$$s(t) = \frac{\ln(200)}{k} + \frac{1}{k} \ln\left(kt + \frac{1}{200}\right)$$

$$s(t_{20}) = 0.5784 + \frac{1}{9.16} \ln\left(9.16(0.00491) + 0.005\right)$$

$$s(t_{20}) = 0.5784 +$$

$$\begin{array}{l} 0.0499756 \\ 0.85 \end{array}$$

$$s(t_{20}) = 25.13$$

$$S(t) = \frac{L(200)}{k} + \frac{1}{k} L\left(kt + \frac{1}{200}\right)$$

$$t_f \Rightarrow \frac{1}{10} = \frac{L(200)}{k} + \frac{1}{k} L\left(kt_f + \frac{1}{200}\right)$$

$$\frac{k}{10} = L\left(200\left(kt_f + \frac{1}{200}\right)\right)$$

$$200kt_f + 1 = e^{\frac{k}{10}}$$

$$200kt_f = e^{\frac{k}{10}} - 1$$

$$t_f = \frac{e^{\frac{k}{10}} - 1}{200k}$$

$$V(t) = \frac{1}{kt + \frac{1}{200}} \quad t_p = \frac{e^{\frac{k}{20}} - 1}{200k}$$

$$V(t_p) = 80 = \frac{1}{k\left(\frac{e^{\frac{k}{20}} - 1}{200k}\right) + \frac{1}{200}}$$

$$80 = \frac{1}{\frac{e^{\frac{k}{20}}}{200} - \frac{1}{200} + \frac{1}{200}}$$

$$80 = \frac{1}{\frac{e^{\frac{k}{20}}}{200}}$$

$$80 = \frac{200}{e^{\frac{k}{20}}}$$

$$e^{\frac{k}{20}} = \frac{200}{80}$$

$$\frac{k}{20} = L\left(\frac{200}{80}\right)$$

$$k = 10 L\left(\frac{200}{80}\right)$$

$$t_p = \frac{e^{L\left(\frac{200}{80}\right)} - 1}{200\left(10 L\left(\frac{200}{80}\right)\right)} \Rightarrow t_p = \frac{\frac{200}{80} - 1}{2000 L\left(\frac{200}{80}\right)}$$

$$t_p = \frac{\frac{200-80}{80}}{2000 L\left(\frac{200}{80}\right)} \Rightarrow \frac{\frac{120}{80}}{2000 L\left(\frac{200}{80}\right)} \Rightarrow 0.0008195$$

$$183.1 t = 0.9$$

$$t = \frac{0.9}{183.1} = 0.00491$$

$$V(t) = \frac{1}{9.16t + 0.005}$$

$$20 = \frac{1}{9.16t + 0.005}$$

$$20(9.16t + 0.005) = 1$$

$$183.2t + 0.1 = 1$$

$$9.1629$$