

> restart

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$$y_g = C_1 + C_2 x + C_3 x^2 + C_4 e^x + C_5 e^{2x} + C_6 \cos(2x) + C_7 \sin(2x)$$

orden = 5 EDO descomulgada

> SolGral := y(x) = C₁ + C₂·x + C₃·x² + C₄·exp(x) + C₅·exp(2 x) + C₆·cos(2 x) + C₇·sin(2 x)

$$\text{SolGral} := y(x) = C_1 + C_2 x + C_3 x^2 + C_4 e^x + C_5 e^{2x} + C_6 \cos(2x) + C_7 \sin(2x) \quad (1)$$

> Sistema := SolGral, diff(SolGral, x), diff(SolGral, x\$2), diff(SolGral, x\$3), diff(SolGral, x\$4), diff(SolGral, x\$5), diff(SolGral, x\$6) : Sistema₁; Sistema₂; Sistema₃; Sistema₄; Sistema₅; Sistema₆; Sistema₇

$$y(x) = C_1 + C_2 x + C_3 x^2 + C_4 e^x + C_5 e^{2x} + C_6 \cos(2x) + C_7 \sin(2x)$$

$$\frac{d}{dx} y(x) = C_2 + 2 C_3 x + C_4 e^x + 2 C_5 e^{2x} - 2 C_6 \sin(2x) + 2 C_7 \cos(2x)$$

$$\frac{d^2}{dx^2} y(x) = 2 C_3 + C_4 e^x + 4 C_5 e^{2x} - 4 C_6 \cos(2x) - 4 C_7 \sin(2x)$$

$$\frac{d^3}{dx^3} y(x) = C_4 e^x + 8 C_5 e^{2x} + 8 C_6 \sin(2x) - 8 C_7 \cos(2x)$$

$$\frac{d^4}{dx^4} y(x) = C_4 e^x + 16 C_5 e^{2x} + 16 C_6 \cos(2x) + 16 C_7 \sin(2x)$$

$$\frac{d^5}{dx^5} y(x) = C_4 e^x + 32 C_5 e^{2x} - 32 C_6 \sin(2x) + 32 C_7 \cos(2x)$$

$$\frac{d^6}{dx^6} y(x) = C_4 e^x + 64 C_5 e^{2x} - 64 C_6 \cos(2x) - 64 C_7 \sin(2x) \quad (2)$$

> Parametro := simplify(solve({Sistema}, {C₁, C₂, C₃, C₄, C₅, C₆, C₇})) : Parametro₁; Parametro₂; Parametro₃; Parametro₄; Parametro₅; Parametro₆; Parametro₇;

$$C_1 = \frac{1}{16} x^2 \left(\frac{d^6}{dx^6} y(x) \right) + \frac{3}{16} \frac{d^6}{dx^6} y(x) - \frac{3}{2} \frac{d^3}{dx^3} y(x) + y(x) - \frac{3}{16} x^2 \left(\frac{d^5}{dx^5} y(x) \right) - \frac{3}{4} \left(\frac{d^3}{dx^3} y(x) \right) x^2 + \frac{3}{8} x^2 \left(\frac{d^4}{dx^4} y(x) \right) - \frac{3}{8} \frac{d^5}{dx^5} y(x) + \frac{1}{2} \left(\frac{d^2}{dx^2} y(x) \right) x^2 + \frac{11}{16} \frac{d^4}{dx^4} y(x) - x \left(\frac{d}{dx} y(x) \right) + \frac{3}{2} \left(\frac{d^3}{dx^3} y(x) \right) x + \frac{7}{16} x \left(\frac{d^5}{dx^5} y(x) \right) - \frac{3}{4} x \left(\frac{d^4}{dx^4} y(x) \right) - \frac{3}{16} x \left(\frac{d^6}{dx^6} y(x) \right)$$

$$C_2 = \frac{d}{dx} y(x) - \frac{3}{2} \frac{d^3}{dx^3} y(x) - \frac{3}{4} x \left(\frac{d^4}{dx^4} y(x) \right) - \frac{1}{8} x \left(\frac{d^6}{dx^6} y(x) \right) + \frac{3}{8} x \left(\frac{d^5}{dx^5} y(x) \right)$$

$$\begin{aligned}
& + \frac{3}{2} \left(\frac{d^3}{dx^3} y(x) \right) x - \frac{7}{16} \frac{d^5}{dx^5} y(x) - \left(\frac{d^2}{dx^2} y(x) \right) x + \frac{3}{4} \frac{d^4}{dx^4} y(x) + \frac{3}{16} \frac{d^6}{dx^6} y(x) \\
C_3 &= \frac{1}{16} \frac{d^6}{dx^6} y(x) - \frac{3}{16} \frac{d^5}{dx^5} y(x) + \frac{3}{8} \frac{d^4}{dx^4} y(x) + \frac{1}{2} \frac{d^2}{dx^2} y(x) - \frac{3}{4} \frac{d^3}{dx^3} y(x) \\
C_4 &= -\frac{1}{5} \left(\frac{d^6}{dx^6} y(x) - 8 \left(\frac{d^3}{dx^3} y(x) \right) - 2 \left(\frac{d^5}{dx^5} y(x) \right) + 4 \left(\frac{d^4}{dx^4} y(x) \right) \right) e^{-x} \\
C_5 &= \frac{1}{64} \left(- \left(\frac{d^5}{dx^5} y(x) \right) - 4 \left(\frac{d^3}{dx^3} y(x) \right) + 4 \left(\frac{d^4}{dx^4} y(x) \right) + \frac{d^6}{dx^6} y(x) \right) e^{-2x} \\
C_6 &= -\frac{3}{320} \cos(2x) \left(\frac{d^5}{dx^5} y(x) \right) - \frac{3}{80} \cos(2x) \left(\frac{d^3}{dx^3} y(x) \right) + \frac{1}{20} \cos(2x) \left(\frac{d^4}{dx^4} y(x) \right) \\
& - \frac{1}{320} \left(\frac{d^6}{dx^6} y(x) \right) \cos(2x) - \frac{11}{320} \sin(2x) \left(\frac{d^5}{dx^5} y(x) \right) \\
& - \frac{1}{80} \sin(2x) \left(\frac{d^3}{dx^3} y(x) \right) + \frac{3}{80} \sin(2x) \left(\frac{d^4}{dx^4} y(x) \right) + \frac{3}{320} \left(\frac{d^6}{dx^6} y(x) \right) \sin(2x) \\
C_7 &= -\frac{3}{320} \sin(2x) \left(\frac{d^5}{dx^5} y(x) \right) - \frac{3}{80} \sin(2x) \left(\frac{d^3}{dx^3} y(x) \right) + \frac{1}{20} \sin(2x) \left(\frac{d^4}{dx^4} y(x) \right) \quad (3) \\
& + \frac{11}{320} \cos(2x) \left(\frac{d^5}{dx^5} y(x) \right) + \frac{1}{80} \cos(2x) \left(\frac{d^3}{dx^3} y(x) \right) - \frac{3}{80} \cos(2x) \left(\frac{d^4}{dx^4} y(x) \right) \\
& - \frac{1}{320} \left(\frac{d^6}{dx^6} y(x) \right) \sin(2x) - \frac{3}{320} \left(\frac{d^6}{dx^6} y(x) \right) \cos(2x)
\end{aligned}$$

> *EcuacionInicial* := simplify(eval(subs($C_1 = rhs(Parametro_1)$, $C_2 = rhs(Parametro_2)$, $C_3 = rhs(Parametro_3)$, $C_4 = rhs(Parametro_4)$, $C_5 = rhs(Parametro_5)$, $C_6 = rhs(Parametro_6)$, $C_7 = rhs(Parametro_7)$, diff(SolGral, x\$7))))

$$\begin{aligned}
EcuacionInicial &:= \frac{d^7}{dx^7} y(x) = 3 \left(\frac{d^6}{dx^6} y(x) \right) - 8 \left(\frac{d^3}{dx^3} y(x) \right) - 6 \left(\frac{d^5}{dx^5} y(x) \right) \\
& + 12 \left(\frac{d^4}{dx^4} y(x) \right) \quad (4)
\end{aligned}$$

> *EcuacionFinal* := lhs(*EcuacionInicial*) - rhs(*EcuacionInicial*) = 0

$$\begin{aligned}
EcuacionFinal &:= \frac{d^7}{dx^7} y(x) - 3 \left(\frac{d^6}{dx^6} y(x) \right) + 8 \left(\frac{d^3}{dx^3} y(x) \right) + 6 \left(\frac{d^5}{dx^5} y(x) \right) \\
& - 12 \left(\frac{d^4}{dx^4} y(x) \right) = 0 \quad (5)
\end{aligned}$$

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