

properties.

$$7) \mathcal{L}^{-1} \{ e^{-as} F(s) \} = f(t-a) \cdot u(t-a)$$

$$8) \mathcal{L} \{ e^{as} f(t) \} = F(s-a)$$

$$9) \mathcal{L}^{-1} \{ F(s) \cdot G(s) \} = f(t) * g(t)$$

operation  
convolution

$$f(t) * g(t) = \int_0^t f(z) \cdot g(t-z) dz$$

Sectional continuous functions

$$\mathcal{L}\{t^2\} = \frac{2!}{s^3}$$

$$\mathcal{L}\{e^{at}f(t)\} = F(s-a)$$

$$\mathcal{L}\{t^2 e^{8t}\} = \frac{2}{(s-8)^3}$$

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$$\mathcal{L}\{e^{2t} \cos(3t)\} = \frac{(s-2)}{(s-2)^2 + (3)^2}$$

$$\mathcal{L}\{\cos(bt)\} = \frac{s}{s^2 + b^2}$$

$$\mathcal{L}^{-1} \left\{ \frac{s}{s^2 - 2s + 2} \right\} = \mathcal{L}^{-1} \left\{ \frac{s}{(s^2 - 2s + 1) + 1} \right\}$$

$$= \mathcal{L}^{-1} \left\{ \frac{s}{(s-1)^2 + (1)^2} \right\}$$

$$= \mathcal{L}^{-1} \left\{ \frac{(s-1) + 1}{(s-1)^2 + (1)^2} \right\}$$

$$= \mathcal{L}^{-1} \left\{ \frac{(s-1)}{(s-1)^2 + (1)^2} \right\} + \mathcal{L}^{-1} \left\{ \frac{1}{(s-1)^2 + (1)^2} \right\}$$

$$\mathcal{L}^{-1} \left\{ \frac{s}{s^2 - 2s + 2} \right\} = e^t \cos(t) + e^t \sin(t)$$

$$\mathcal{L} \{ e^{at} f(t) \} = F(s-a) \left\{ \begin{array}{l} \mathcal{L} \{ \cos(bt) \} = \frac{s}{s^2 + b^2} \\ \mathcal{L} \{ \sin(bt) \} = \frac{b}{s^2 + b^2} \end{array} \right\}$$

$$\mathcal{L}^{-1} \left\{ \frac{e^{3s}}{s^2 + 9} \right\} =$$

$$\begin{aligned} \mathcal{L}^{-1} \left\{ \frac{1}{s^2 + 9} \right\} &= \frac{1}{3} \mathcal{L}^{-1} \left\{ \frac{3}{s^2 + 9} \right\} \\ &= \frac{1}{3} \left( \sin(3t) \right) \end{aligned}$$

$$\mathcal{L}^{-1} \left\{ \frac{e^{3s}}{s^2 + 9} \right\} = \frac{1}{3} \sin(3(t+3)) \cdot u(t+3)$$

$$\mathcal{L}^{-1} \left\{ e^{-as} \cdot F(s) \right\} = f(t-a) \cdot u(t-a)$$

$$\mathcal{L}^{-1} \left\{ \frac{s}{(s^2 + 16)^2} \right\} = \mathcal{L}^{-1} \left\{ \frac{s}{s^2 + 16} \cdot \frac{1}{s^2 + 16} \right\}$$

$$= \frac{1}{4} \mathcal{L}^{-1} \left\{ \frac{s}{s^2 + 16} \cdot \frac{4}{s^2 + 16} \right\}$$

$$\mathcal{L}^{-1} \left\{ \frac{s}{s^2 + 16} \right\} = \cos(4t)$$

$$\mathcal{L}^{-1} \left\{ \frac{4}{s^2 + 16} \right\} = \sin(4t)$$

$$\mathcal{L}^{-1} \{ F(s) \cdot G(s) \} = f(t) * g(t)$$

$$\frac{1}{4} \mathcal{L}^{-1} \left\{ \frac{s}{s^2 + 16} \cdot \frac{4}{s^2 + 16} \right\} = \cos(4t) * \sin(4t)$$

$$\frac{1}{4} \cos(4t) * \sin(4t) = \int_0^t \cos(4z) \cdot \sin(4(t-z)) dz$$

$$\frac{1}{4} \int_0^t \cos(4z) \left[ \sin(4t) \cos(4z) - \cos(4t) \sin(4z) \right] dz$$

$$\frac{1}{4} \left( \sin(4t) \int_0^t \cos^2(4z) dz - \cos(4t) \int_0^t \cos(4z) \sin(4z) dz \right)$$

$$\frac{1}{4} \left( \sin(4t) \int_0^t \left( \frac{1}{2} + \frac{1}{2} \cos(8z) \right) dz - \frac{\cos(4t)}{4} \int_0^t \sin(4z) \cos(4z) 4 dz \right)$$

$$\frac{1}{4} \left( \frac{\sin(4t)}{2} \int_0^t dz + \frac{\sin(4t)}{16} \int_0^t \cos(8z) 8 dz - \frac{\cos(4t)}{4} \left( \frac{\sin^2(4z)}{2} \right) \Big|_0^t \right)$$

$$\frac{1}{4} \left( \frac{\sin(4t)}{2} \left( t - 0 \right) + \frac{\sin(4t)}{16} \left( \sin(8z) \right) \Big|_0^t - \frac{\cos(4t)}{4} \left( \frac{\sin^2(4z)}{2} \right) \Big|_0^t \right)$$

$$\frac{1}{4} \left( \frac{\sin(4t)}{2} [t - 0] + \frac{\sin(4t)}{16} [\sin(8t) - 0] - \frac{\cos(4t)}{4} \left( \frac{\sin^2(4t)}{2} - 0 \right) \right)$$

$$\frac{1}{4} \left( \frac{t \sin(4t)}{2} + \frac{\sin(4t)}{16} (2 \sin(4t) \cos(4t)) - \frac{\cos(4t)}{8} (\sin^2(4t)) \right)$$

$$\frac{1}{4} \left( \frac{t \sin(4t)}{2} + \frac{\sin^2(4t) \cos(4t)}{8} - \frac{\sin^2(4t) \cos(4t)}{8} \right)$$

$$\mathcal{L}^{-1} \left\{ \frac{s}{(s^2 + 16)^2} \right\} = \frac{t \sin(4t)}{2}$$

$$\mathcal{L}\{f(t)\} = F(s)$$

$$f, t \in \mathbb{R}$$

$$F \in \mathbb{R}$$

$$s \in \mathbb{C}$$

$$\mathcal{L}^{-1}\{F(s)\} = f(t)$$

$$F \in \mathbb{R}$$

$$s \in \mathbb{C}$$

$$f, t \in \mathbb{R}$$

$$\text{Ecuacion} := \frac{d}{dt} y(t) + \int_0^t y(v) e^{-2t+2v} dv = 1$$

$$\frac{dy}{dt} + \int_0^t y(z) e^{-2(t-z)} dz = 1$$

$$\mathcal{L}\left\{\frac{dy}{dt}\right\} + \mathcal{L}\{y(t)\} \cdot \mathcal{L}\{e^{-2t}\} = \mathcal{L}\{1\}$$

$$\mathcal{L}\{y(t)\} - y(0) + \mathcal{L}\{y(t)\} \cdot \left(\frac{1}{s+2}\right) = \frac{1}{s}$$

$$\mathcal{L}\{y(t)\} \left(1 + \frac{1}{s+2}\right) = \frac{1}{s} + 1$$

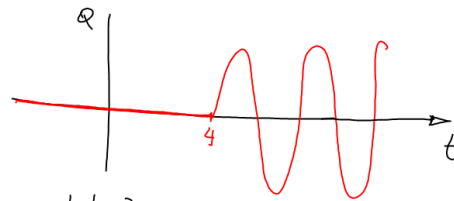
$$\mathcal{L}\{y(t)\} = \frac{\frac{1}{s} + 1}{1 + \frac{1}{s+2}}$$

$$= \frac{\frac{1+s}{s}}{\frac{s+2+1}{s+2}}$$

$$\mathcal{L}\{y(t)\} = \frac{(s+1)(s+2)}{s(s+3)}$$

math rep. Electrical Switch

$$\frac{d^2 y}{dt^2} - \frac{dy}{dt} + y = u(t-4) \cdot \sin(60\pi(t-4))$$



$$y(0) = 0$$

$$y'(0) = 1$$

$$\mathcal{L}\left\{\frac{d^2 y}{dt^2}\right\} - \mathcal{L}\left\{\frac{dy}{dt}\right\} + \mathcal{L}\{y\} = \mathcal{L}\{u(t-4)\sin(60\pi(t-4))\}$$

$$\left(s^2 \mathcal{L}\{y\} - s(0) - (1)\right) - (s \mathcal{L}\{y\} - (0)) + \mathcal{L}\{y\} =$$

$$\frac{e^{-4s} 60\pi}{s^2 + 3600\pi^2}$$

$$\mathcal{L}\{\sin(60\pi t)\} = \frac{60\pi}{s^2 + 3600\pi^2}$$

$$(s^2 - s + 1) \mathcal{L}\{y\} = 60\pi \frac{e^{-4s}}{s^2 + 3600\pi^2} + 1$$

$$(s^2 - s + 1) \mathcal{L}\{y\} = \frac{s^2 + 3600\pi^2 + 60\pi e^{-4s}}{s^2 + 3600\pi^2}$$

$$\mathcal{L}\{y\} = \frac{s^2 + (3600\pi^2 + 60\pi e^{-4s})}{(s^2 + 3600\pi^2)(s^2 - s + 1)}$$

$$\frac{s^2 + (3600\pi^2 + 60\pi e^{-4s})}{(s^2 + 3600\pi^2)(s^2 - s + 1)} = \frac{As + B}{s^2 + 3600\pi^2} + \frac{Cs + D}{s^2 - s + 1}$$

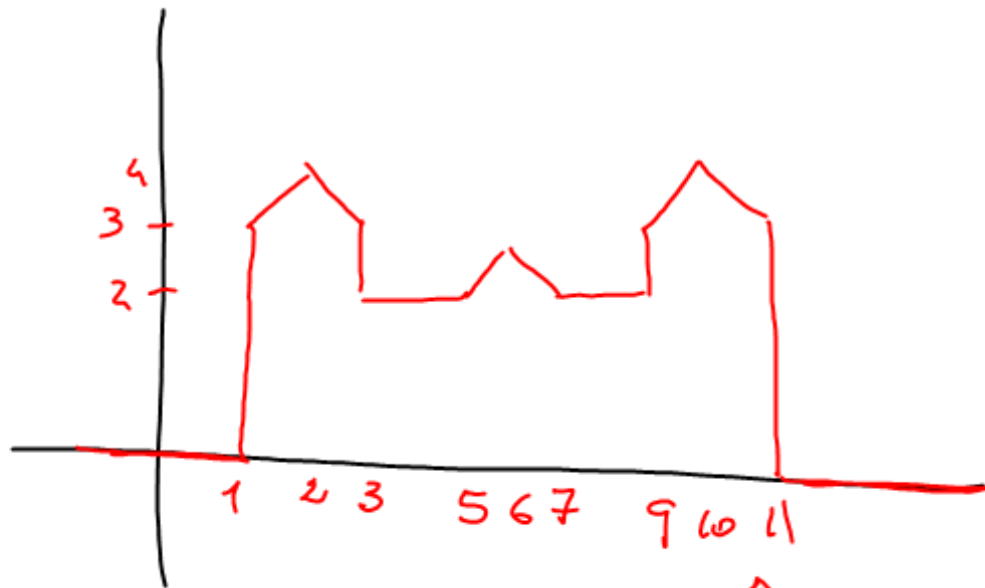
$$+ \frac{Cs + D}{(s^2 - s + \frac{3}{4}) + \frac{3}{4}}$$

$$\cos(60\pi t) \quad \sin(60\pi t)$$

$$+ \frac{Cs + D}{(s - \frac{1}{2})^2 + (\frac{\sqrt{3}}{2})^2}$$

$$e^{\frac{1}{2}t} \cos\left(\frac{\sqrt{3}}{2}t\right) \quad e^{\frac{1}{2}t} \sin\left(\frac{\sqrt{3}}{2}t\right)$$





$$u(t-a) =$$



$$r(t-a) =$$

