

> restart

$$\frac{dy_1}{dt} = 2y_1 + 3y_2 + 5e^{2t}$$

$$y_1(0) = 3$$

$$\frac{dy_2}{dt} = y_1 + 4y_2 - 6e^{-t}$$

$$y_2(0) = -2$$

> Sistema := diff(y₁(t), t) = 2·y₁(t) + 3·y₂(t) + 5·exp(2 t), diff(y₂(t), t) = y₁(t) + 4·y₂(t) - 6·exp(-t) : Sistema₁; Sistema₂

$$\frac{d}{dt} y_1(t) = 2 y_1(t) + 3 y_2(t) + 5 e^{2t}$$

$$\frac{d}{dt} y_2(t) = y_1(t) + 4 y_2(t) - 6 e^{-t} \quad (1)$$

> Condiciones := y₁(0) = 3, y₂(0) = -2

$$\text{Condiciones} := y_1(0) = 3, y_2(0) = -2 \quad (2)$$

> Solucion := dsolve({Sistema, Condiciones}) : Solucion₁; Solucion₂

$$y_1(t) = \frac{9}{4} e^t - \frac{13}{12} e^{5t} + \frac{10}{3} e^{2t} - \frac{3}{2} e^{-t}$$

$$y_2(t) = -\frac{3}{4} e^t - \frac{13}{12} e^{5t} + \frac{3}{2} e^{-t} - \frac{5}{3} e^{2t} \quad (3)$$

> AA := array([[2, 3], [1, 4]])

$$AA := \begin{bmatrix} 2 & 3 \\ 1 & 4 \end{bmatrix} \quad (4)$$

> Ycero := array([3, -2])

$$Ycero := \begin{bmatrix} 3 & -2 \end{bmatrix} \quad (5)$$

> Btau := array([5·exp(2·tau), -6·exp(-tau)])

$$Btau := \begin{bmatrix} 5 e^{2\tau} & -6 e^{-\tau} \end{bmatrix} \quad (6)$$

> with(linalg) :

> MatExp := exponential(AA, t)

$$MatExp := \begin{bmatrix} \frac{3}{4} e^t + \frac{1}{4} e^{5t} & \frac{3}{4} e^{5t} - \frac{3}{4} e^t \\ \frac{1}{4} e^{5t} - \frac{1}{4} e^t & \frac{1}{4} e^t + \frac{3}{4} e^{5t} \end{bmatrix} \quad (7)$$

> MatExpTau := exponential(AA, t - tau)

$$MatExpTau := \begin{bmatrix} \frac{3}{4} e^{t-\tau} + \frac{1}{4} e^{5t-5\tau} & \frac{3}{4} e^{5t-5\tau} - \frac{3}{4} e^{t-\tau} \\ \frac{1}{4} e^{5t-5\tau} - \frac{1}{4} e^{t-\tau} & \frac{1}{4} e^{t-\tau} + \frac{3}{4} e^{5t-5\tau} \end{bmatrix} \quad (8)$$

$$\begin{aligned} &> MatBtau := simplify(evalm(MatExpTau \&* Btau)) : MatBtau_1; MatBtau_2 \\ &\quad \frac{15}{4} e^{\tau+t} + \frac{5}{4} e^{-3\tau+5t} - \frac{9}{2} e^{-6\tau+5t} + \frac{9}{2} e^{-2\tau+t} \\ &\quad \frac{5}{4} e^{-3\tau+5t} - \frac{5}{4} e^{\tau+t} - \frac{3}{2} e^{-2\tau+t} - \frac{9}{2} e^{-6\tau+5t} \end{aligned} \quad (9)$$

$$\begin{aligned} &> IntMatBtau := map(int, MatBtau, tau=0..t) : IntMatBtau_1; IntMatBtau_2 \\ &\quad -\frac{3}{2} e^t - \frac{1}{3} e^{5t} + \frac{10}{3} e^{2t} - \frac{3}{2} e^{-t} \\ &\quad -\frac{1}{3} e^{5t} + \frac{1}{2} e^t - \frac{5}{3} e^{2t} + \frac{3}{2} e^{-t} \end{aligned} \quad (10)$$

$$\begin{aligned} &> Ceros := map(rcurry(eval, t=0'), IntMatBtau) \\ &\quad Ceros := \begin{bmatrix} 0 & 0 \end{bmatrix} \end{aligned} \quad (11)$$

$$\begin{aligned} &> SOL := evalm(evalm(MatExp \&* Ycero) + IntMatBtau) : yy_1(t) = SOL_1; yy_2(t) = SOL_2 \\ &\quad yy_1(t) = \frac{9}{4} e^t - \frac{13}{12} e^{5t} + \frac{10}{3} e^{2t} - \frac{3}{2} e^{-t} \\ &\quad yy_2(t) = -\frac{3}{4} e^t - \frac{13}{12} e^{5t} + \frac{3}{2} e^{-t} - \frac{5}{3} e^{2t} \end{aligned} \quad (12)$$

$$\begin{aligned} &> Solucion_1; Solucion_2 \\ &\quad y_1(t) = \frac{9}{4} e^t - \frac{13}{12} e^{5t} + \frac{10}{3} e^{2t} - \frac{3}{2} e^{-t} \\ &\quad y_2(t) = -\frac{3}{4} e^t - \frac{13}{12} e^{5t} + \frac{3}{2} e^{-t} - \frac{5}{3} e^{2t} \end{aligned} \quad (13)$$

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