

> restart

> EcuacionDiferencial := diff(y(t), t, t) + g = 0

$$\text{EcuacionDiferencial} := \frac{d^2}{dt^2} y(t) + g = 0 \quad (1)$$

> Solucion := dsolve(EcuacionDiferencial, y(t))

$$\text{Solucion} := y(t) = -\frac{1}{2} g t^2 + \_C1 t + \_C2 \quad (2)$$

> DerivadaSolucion := diff(Solucion, t)

$$\text{DerivadaSolucion} := \frac{d}{dt} y(t) = -g t + \_C1 \quad (3)$$

> DerivadaSegundaSolucion := diff(DerivadaSolucion, t)

$$\text{DerivadaSegundaSolucion} := \frac{d^2}{dt^2} y(t) = -g \quad (4)$$

> Comprobar := subs(DerivadaSegundaSolucion, EcuacionDiferencial)

$$\text{Comprobar} := 0 = 0 \quad (5)$$

> restart

> Digits := 4

$$\text{Digits} := 4 \quad (6)$$

problema de la flecha y el arco

> Modelo1 :=  $\left( \frac{0.030}{9.8067} \right) \text{diff}(s(t), t, t) = - \left( \frac{14.61}{0.40} \right) \cdot s(t)$

$$\text{Modelo1} := 0.003059 \left( \frac{d^2}{dt^2} s(t) \right) = -36.52 s(t) \quad (7)$$

> EcuacionDiferencial := lhs(Modelo1) - rhs(Modelo1) = 0

$$\text{EcuacionDiferencial} := 0.003059 \left( \frac{d^2}{dt^2} s(t) \right) + 36.52 s(t) = 0 \quad (8)$$

> Solucion1 := dsolve({Modelo1, s(0) = -0.436, D(s)(0) = 0})

$$\text{Solucion1} := s(t) = -\frac{109}{250} \cos\left(\frac{200}{3059} \sqrt{2792867} t\right) \quad (9)$$

> evalf(%)

$$s(t) = -0.4360 \cos(109.2 t) \quad (10)$$

> TiempoRecorrido := solve(rhs(Solucion1) = 0, t)

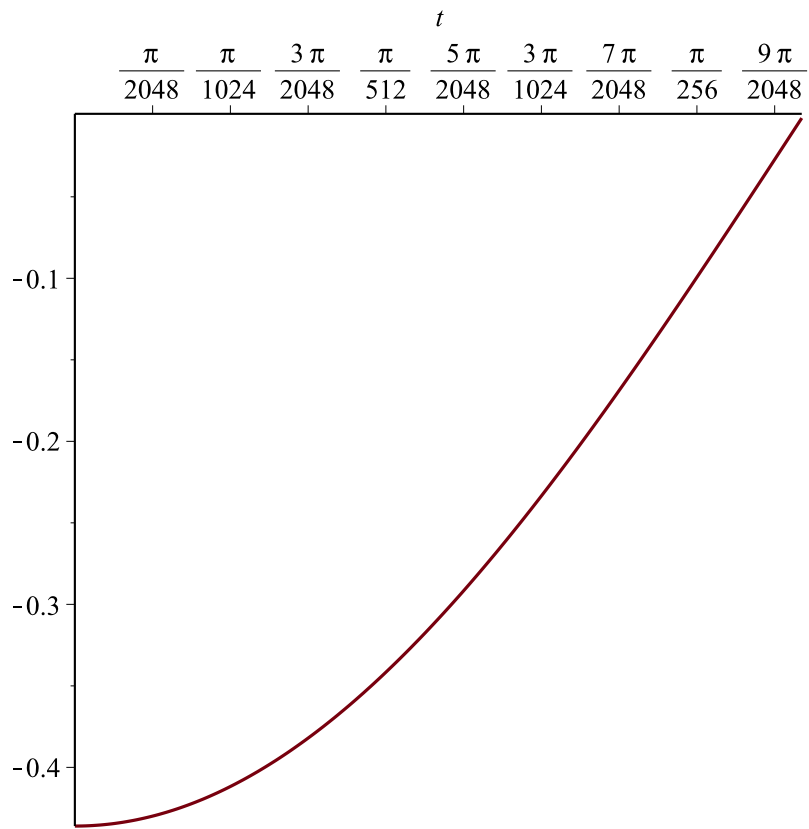
$$\text{TiempoRecorrido} := \frac{1}{365200} \pi \sqrt{2792867} \quad (11)$$

> evalf(%)

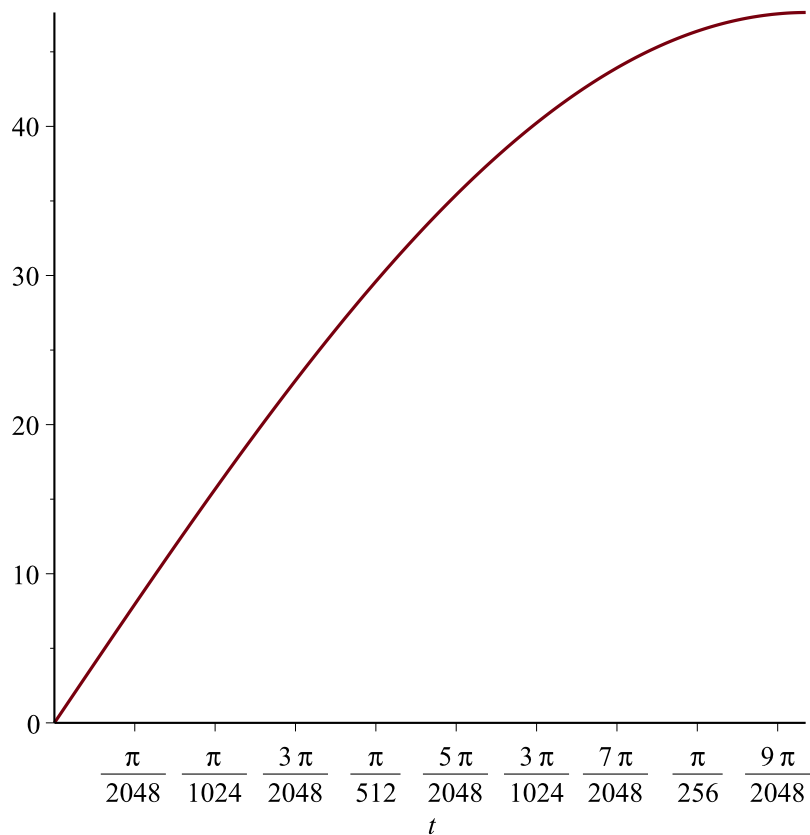
$$0.01437 \quad (12)$$

(segundos)

> plot(rhs(Solucion1), t = 0 .. TiempoRecorrido)



> `plot(rhs(diff(SolucionI, t)), t=0..TiempoRecorrido)`



>  $VelocidadInicial := rhs(subs(t = TiempoRecorrido, diff(Solucion1, t)))$

$$VelocidadInicial := \frac{436}{15295} \sin\left(\frac{1}{2} \pi\right) \sqrt{2792867} \quad (13)$$

>  $evalf(\%)$

$$47.64 \quad (14)$$

(metros/segundos)

>  $evalf(\%) \cdot 3.6$

$$171.5 \quad (15)$$

(Kilómetros/hora)

>  
Continuando con la clase anterior  
TIRO PARABÓLICO

>  $EcuaVertical := diff(y(t), t, t) = -9.8067$

$$EcuaVertical := \frac{d^2}{dt^2} y(t) = -9.8067 \quad (16)$$

>  $evalf(Pi); eval(pi); eval(PI)$

$$3.142$$

$$\pi$$

$$\Pi \quad (17)$$

$$\begin{aligned} &> \text{EcuaHorizontal} := \text{diff}(x(t), t) = \text{VelocidadInicial} \cdot \cos\left(\frac{\text{Pi}}{4}\right) \\ &\quad \text{EcuaHorizontal} := \frac{d}{dt} x(t) = \frac{218}{15295} \sqrt{2792867} \sqrt{2} \end{aligned} \quad (18)$$

$$\begin{aligned} &> \text{evalf}(\%, 4) \\ &\quad \frac{d}{dt} x(t) = 33.67 \end{aligned} \quad (19)$$

$$\begin{aligned} &> \text{SolucionVertical} := \text{dsolve}\left(\left\{\text{EcuaVertical}, y(0) = 2.0, D(y)(0) = \text{VelocidadInicial} \cdot \sin\left(\frac{\text{Pi}}{4}\right)\right\}\right) \\ &\quad \text{SolucionVertical} := y(t) = -\frac{98067}{20000} t^2 + \frac{218}{15295} \sqrt{2792867} \sqrt{2} t + 2 \end{aligned} \quad (20)$$

$$\begin{aligned} &> \text{evalf}(\%, 4) \\ &\quad y(t) = -4.903 t^2 + 33.67 t + 2. \end{aligned} \quad (21)$$

$$\begin{aligned} &> \text{SolucionHorizontal} := \text{dsolve}(\{\text{EcuaHorizontal}, x(0) = 5\}) \\ &\quad \text{SolucionHorizontal} := x(t) = \frac{218}{15295} \sqrt{5585734} t + 5 \end{aligned} \quad (22)$$

$$\begin{aligned} &> \text{evalf}(\%, 4) \\ &\quad x(t) = 33.67 t + 5. \end{aligned} \quad (23)$$

$$\begin{aligned} &> \text{TiempoVuelo} := \text{solve}(\text{rhs}(\text{SolucionVertical}) = 0, t) \\ &\quad \text{TiempoVuelo} := \frac{436000}{299986953} \sqrt{2792867} \sqrt{2} - \frac{200}{299986953} \sqrt{27463302350827}, \\ &\quad \frac{436000}{299986953} \sqrt{2792867} \sqrt{2} + \frac{200}{299986953} \sqrt{27463302350827} \end{aligned} \quad (24)$$

$$\begin{aligned} &> \text{evalf}(\%, 4) \\ &\quad -0.061, 6.927 \end{aligned} \quad (25)$$

$$\begin{aligned} &> \text{evalf}(\text{TiempoVuelo}[2]) \\ &\quad 6.927 \end{aligned} \quad (26)$$

(segundos)

$$\begin{aligned} &> \text{DistanciaMaxima} := \text{subs}(t = \text{TiempoVuelo}[2], \text{rhs}(\text{SolucionHorizontal})) \\ &\quad \text{DistanciaMaxima} := \frac{218}{15295} \sqrt{5585734} \left( \frac{436000}{299986953} \sqrt{2792867} \sqrt{2} \right. \\ &\quad \left. + \frac{200}{299986953} \sqrt{27463302350827} \right) + 5 \end{aligned} \quad (27)$$

$$\begin{aligned} &> \text{evalf}(\%, 5) \\ &\quad 238.41 \end{aligned} \quad (28)$$

( metros )

$$\begin{aligned} &> \text{TiempoAlturaMaxima} := \text{solve}(\text{rhs}(\text{diff}(\text{SolucionVertical}, t)) = 0, t) \\ &\quad \text{TiempoAlturaMaxima} := \frac{436000}{299986953} \sqrt{2792867} \sqrt{2} \end{aligned} \quad (29)$$

$$\begin{aligned} &> \text{evalf}(\%) \\ &\quad 3.433 \end{aligned} \quad (30)$$

( segundos )

$$> \text{AlturaMaxima} := \text{subs}(t = \text{TiempoAlturaMaxima}, \text{rhs}(\text{SolucionVertical}))$$

$$AlturaMaxima := \frac{17955738706}{299986953} \quad (31)$$

$$\begin{aligned} &> evalf(\%) \\ &59.86 \quad (32) \\ & \quad \quad \quad (\text{ metros }) \end{aligned}$$

>