

> restart

PROBLEMA DEL ARCO Y LA FLECHA

> EcuaDinamica := -Hooke·s(t) = Masa·diff(s(t), t\$2)

$$EcuaDinamica := -Hooke s(t) = Masa \left(\frac{d^2}{dt^2} s(t) \right) \quad (1)$$

> Condicion := s(0) = -\frac{392}{1000}, D(s)(0) = 0

$$Condicion := s(0) = -\frac{49}{125}, D(s)(0) = 0 \quad (2)$$

> Hooke := \frac{\left(\frac{1348}{100}\right)}{\frac{35}{100}}; Masa := \frac{\left(\frac{16}{1000}\right)}{\frac{981}{100}};

$$Hooke := \frac{1348}{35}$$

$$Masa := \frac{8}{4905} \quad (3)$$

> EcuaDinamica, evalf(%, 3)

$$-\frac{1348}{35} s(t) = \frac{8}{4905} \frac{d^2}{dt^2} s(t)$$

$$-38.5 s(t) = 0.00163 \left(\frac{d^2}{dt^2} s(t) \right) \quad (4)$$

> Solucion := dsolve({EcuaDinamica, Condicion}); evalf(%, 3); subs(t=0, rhs(Solucion)); evalf(%, 3)

$$Solucion := s(t) = -\frac{49}{125} \cos\left(\frac{3}{14} \sqrt{514262} t\right)$$

$$s(t) = -0.392 \cos(153. t)$$

$$-\frac{49}{125} \cos(0)$$

$$-0.392 \quad (5)$$

> DerSol := diff(Solucion, t); evalf(%, 3); subs(t=0, rhs(DerSol)); evalf(%, 3)

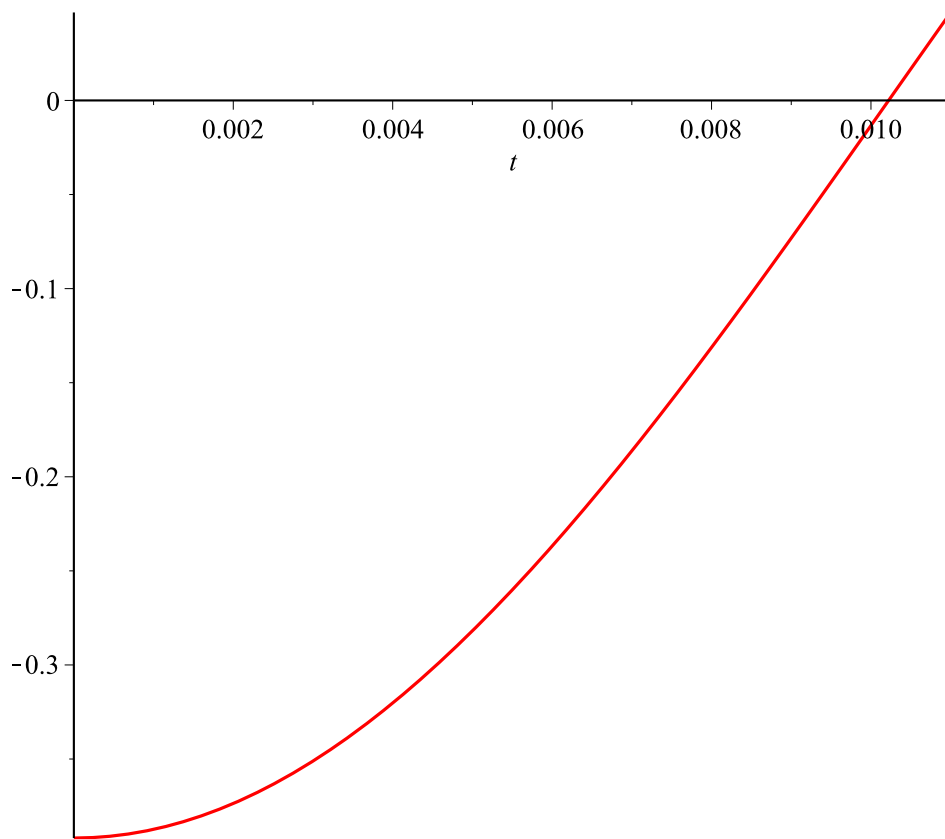
$$DerSol := \frac{d}{dt} s(t) = \frac{21}{250} \sin\left(\frac{3}{14} \sqrt{514262} t\right) \sqrt{514262}$$

$$\frac{d}{dt} s(t) = 60.2 \sin(153. t)$$

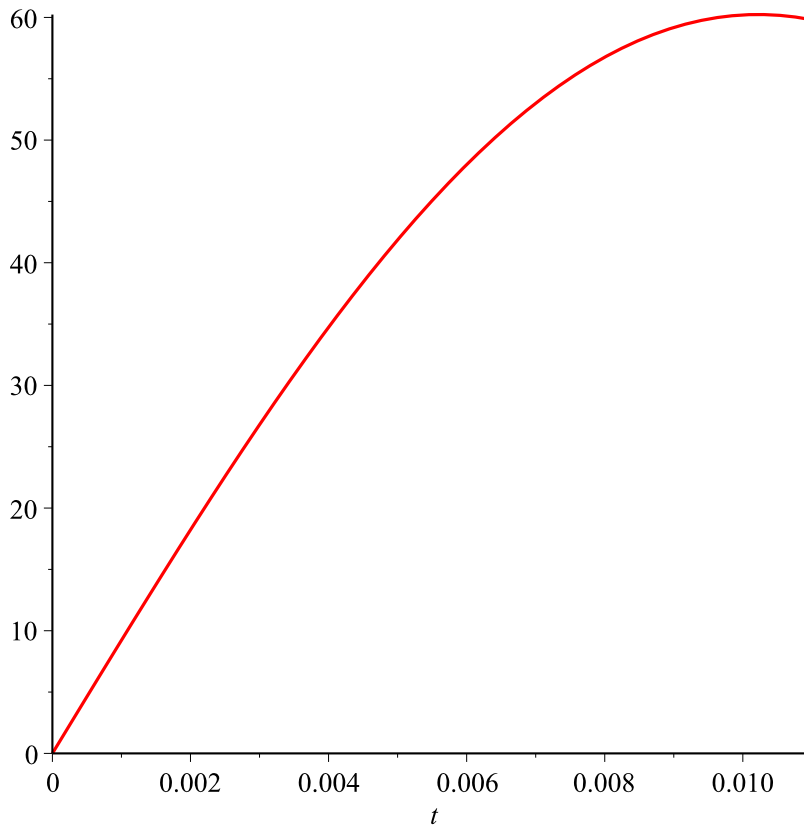
$$\frac{21}{250} \sin(0) \sqrt{514262}$$

$$0. \quad (6)$$

> plot(rhs(Solucion), t=0..0.011)



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=  
> plot(rhs(diff(Solucion, t)), t=0..0.011)
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$$\begin{aligned} &> \text{TiempoEmpuje} := \text{solve}(\text{rhs}(\text{Solucion}) = 0) : \text{evalf}(\%); \\ &\quad \quad \quad 0.01022196621 \end{aligned} \quad (7)$$

$$\begin{aligned} &> \text{Velocidad} := \text{subs}(t = \text{TiempoEmpuje}, \text{rhs}(\text{diff}(\text{Solucion}, t))); \text{evalf}(\%, 4); \text{evalf}(\%, 4) \cdot 3.6 \\ &\quad \quad \quad \text{Velocidad} := \frac{21}{250} \sin\left(\frac{1}{2} \pi\right) \sqrt{514262} \\ &\quad \quad \quad 60.24 \\ &\quad \quad \quad 216.864 \end{aligned} \quad (8)$$

TIRO PARABÓLICO

$$\begin{aligned} &> \text{EcuaVertical} := \text{diff}(y(t), t\$2) = -\frac{981}{100} \\ &\quad \quad \quad \text{EcuaVertical} := \frac{d^2}{dt^2} y(t) = -\frac{981}{100} \end{aligned} \quad (9)$$

$$\begin{aligned} &> \text{EcuaHoriz} := \text{diff}(x(t), t) = \text{Velocidad} \cdot \cos\left(\frac{\text{Pi}}{4}\right) \\ &\quad \quad \quad \text{EcuaHoriz} := \frac{d}{dt} x(t) = \frac{21}{500} \sqrt{514262} \sqrt{2} \end{aligned} \quad (10)$$

$$\begin{aligned} > \text{CondVertical} := y(0) = 2, D(y)(0) = \text{Velocidad} \cdot \sin\left(\frac{\text{Pi}}{4}\right) \\ &\quad \text{CondVertical} := y(0) = 2, D(y)(0) = \frac{21}{500} \sqrt{514262} \sqrt{2} \end{aligned} \quad (11)$$

$$\begin{aligned} > \text{CondHoriz} := x(0) = 5 \\ &\quad \text{CondHoriz} := x(0) = 5 \end{aligned} \quad (12)$$

$$\begin{aligned} > \text{SolVert} := \text{dsolve}(\{\text{EcuVertical}, \text{CondVertical}\}); \text{evalf}(\%, 3) \\ &\quad \text{SolVert} := y(t) = -\frac{981}{200} t^2 + \frac{21}{500} \sqrt{514262} \sqrt{2} t + 2 \\ &\quad y(t) = -4.90 t^2 + 42.4 t + 2. \end{aligned} \quad (13)$$

$$\begin{aligned} > \text{SolHoriz} := \text{dsolve}(\{\text{EcuHoriz}, \text{CondHoriz}\}); \text{evalf}(\%, 3) \\ &\quad \text{SolHoriz} := x(t) = \frac{21}{250} \sqrt{257131} t + 5 \\ &\quad x(t) = 42.6 t + 5. \end{aligned} \quad (14)$$

$$\begin{aligned} > \text{TiempoVuelo} := \text{solve}(\text{rhs}(\text{SolVert}) = 0); \text{evalf}(\%, 5) \\ \text{TiempoVuelo} := \frac{14}{1635} \sqrt{257131} - \frac{2}{1635} \sqrt{12871919}, \frac{14}{1635} \sqrt{257131} \\ &\quad + \frac{2}{1635} \sqrt{12871919} \\ &\quad -0.0466, 8.7306 \end{aligned} \quad (15)$$

$$\begin{aligned} > \text{DistanciaFinal} := \text{subs}(t = \text{TiempoVuelo}[2], \text{rhs}(\text{SolHoriz})); \text{evalf}(\%, 6) \\ \text{DistanciaFinal} := \frac{21}{250} \sqrt{257131} \left(\frac{14}{1635} \sqrt{257131} + \frac{2}{1635} \sqrt{12871919} \right) + 5 \\ &\quad 376.881 \end{aligned} \quad (16)$$

$$\begin{aligned} > \text{TiempoAlturaMax} := \text{solve}(\text{rhs}(\text{diff}(\text{SolVert}, t)) = 0); \text{evalf}(\%) \\ \text{TiempoAlturaMax} := \frac{7}{1635} \sqrt{514262} \sqrt{2} \\ &\quad 4.341976796 \end{aligned} \quad (17)$$

$$\begin{aligned} > \text{AlturaMax} := \text{subs}(t = \text{TiempoAlturaMax}, \text{rhs}(\text{SolVert})); \text{evalf}(\%) \\ \text{AlturaMax} := \frac{118091}{1250} \\ &\quad 94.47280000 \end{aligned} \quad (18)$$

$$> \text{plot}([\text{rhs}(\text{SolHoriz}), \text{rhs}(\text{SolVert}), t = 0 .. \text{TiempoVuelo}[2]], \text{scaling} = \text{CONSTRAINED})$$

