

EDO(1)NL

$$\frac{dy}{dx} = f(x, y)$$

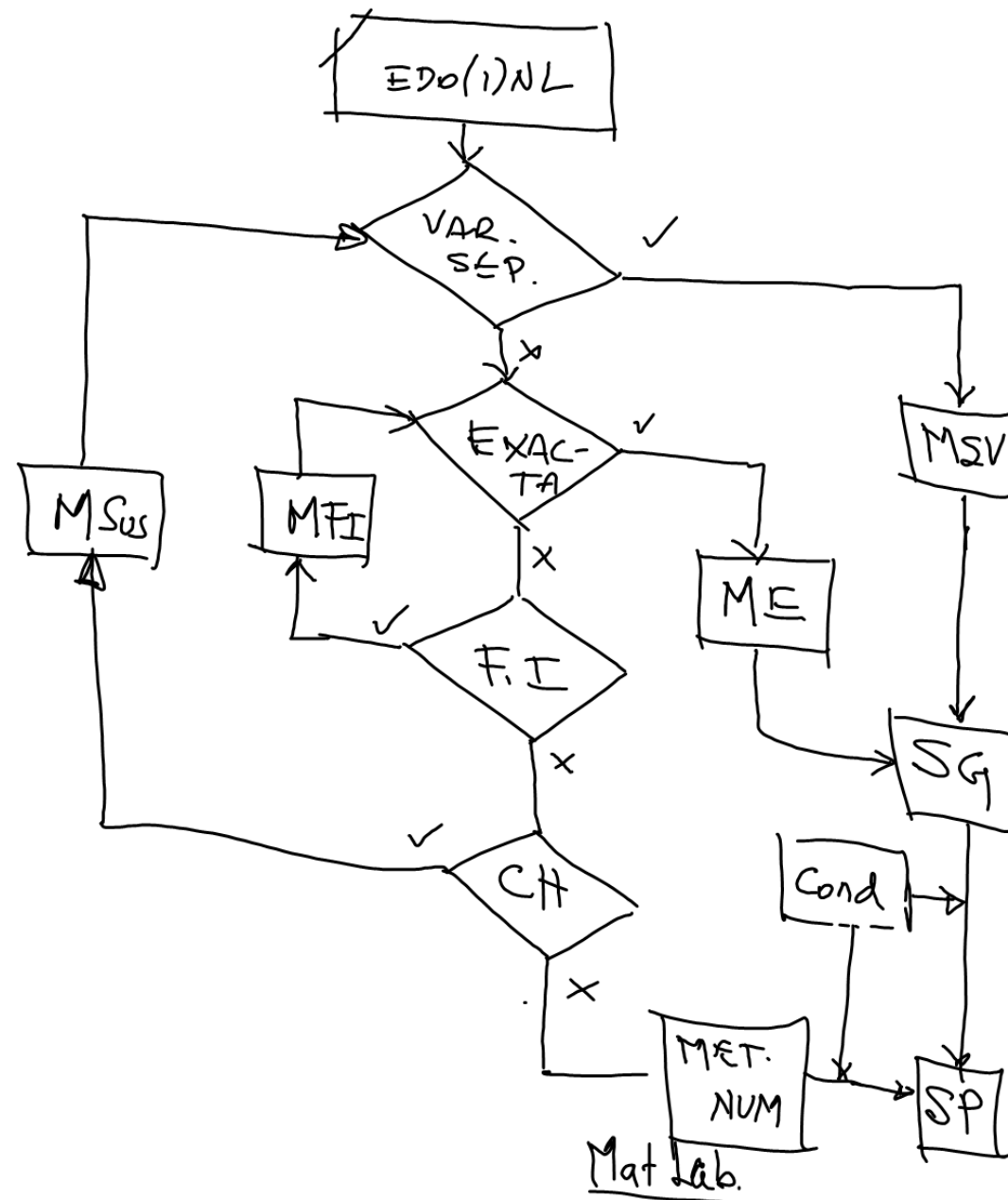
$$\frac{dy}{dx} = - \frac{M(x, y)}{N(x, y)}$$

$$N \frac{dy}{dx} = -M$$

$$M + N \frac{dy}{dx} = 0$$

FORMA GENERAL

PROCEDIMIENTO SOLUCIÓN EDO(1)NL



MÉTODO DE VARIABLES SEPARABLES.

$$M(x, y) + N(x, y) \frac{dy}{dx} = 0$$

$$\Rightarrow P(x) \cdot Q(y) + R(x) \cdot S(y) \cdot \frac{dy}{dx} = 0$$

multiplicamos

$$\left(\frac{1}{Q(y)R(x)} \right)$$

$$\frac{\cancel{P(x)} \cancel{Q(y)}}{\cancel{Q(y)} \cancel{R(x)}} + \frac{\cancel{R(x)} \cancel{S(y)}}{\cancel{Q(y)} \cancel{R(x)}} \frac{dy}{dx} = 0$$

$$\frac{P(x)}{R(x)} + \frac{S(y)}{Q(y)} \cdot \frac{dy}{dx} = 0$$

mult. dx

$$\frac{P(x)}{R(x)} dx + \frac{S(y)}{Q(y)} \cdot \frac{dy}{dx} \cdot dx = 0$$

$$\frac{P(x)}{R(x)} dx + \frac{S(y)}{Q(y)} dy = 0$$

$$\frac{S(y)}{Q(y)} dy = -\frac{P(x)}{R(x)} dx$$

$$\int \frac{S(y)}{Q(y)} dy = -\int \frac{P(x)}{R(x)} dx$$

$$\left[\int \frac{S(y)}{Q(y)} dy \right] + C_1 = \left[-\int \frac{P(x)}{R(x)} dx \right] + C_2$$

$$\left[\int \frac{S(y)}{Q(y)} dy \right] + \left[\int \frac{P(x)}{R(x)} dx \right] = C_2 - C_1$$

$$\boxed{\Phi(x, y) = C} \quad \begin{array}{l} \text{SG} \\ \text{BDO(1)NL} \end{array}$$

$$M(x, y) + N(x, y) \frac{dy}{dx} = 0$$

Variables
separables.

BDO(1)NL.

$$(y^2 + xy^2) \cdot \frac{dy}{dx} + (x^2 - yx^2) = 0$$

$N(x, y)$ $M(x, y)$

$$(1+x)y^2 \cdot \frac{dy}{dx} + x^2(1-y) = 0$$

$$R(x) S(y) \cdot \frac{dy}{dx} + P(x) Q(y) = 0$$

$$\frac{1}{R(x)Q(y)} \cdot \frac{(1+x)y^2}{(1+x)(1-y)} \left(\frac{dy}{dx} \right) + \frac{x^2(1-y)}{(1+x)(1-y)} = 0$$

$$\frac{y^2}{1-y} \cdot \frac{dy}{dx} + \frac{x^2}{1+x} = 0$$

$$\frac{y^2}{1-y} \cdot \frac{dy}{dx} = -\frac{x^2}{1+x}$$

$$\begin{array}{r} x^2 \overline{) 1+x} \\ -x^2-x \\ \hline 0-x \\ +x+1 \\ \hline 0 \end{array} \quad \uparrow$$

$$\frac{y^2}{1-y} dy = -\frac{x^2}{1+x} dx$$

$$\int \frac{y^2}{1-y} dy = -\int \frac{x^2}{1+x} dx$$

$$\begin{array}{r} y^2 \overline{) 1-y} \\ -y^2+y-y-1 \\ \hline 0 \end{array} \quad \downarrow$$

$$-\int y dy - \int dy - \int \frac{-dy}{1-y} = -\left(\int x dx - \int dx + \int \frac{dx}{1+x} \right)$$

$$-\frac{y^2}{2} - y - \ln(1-y) + C_1 = -\frac{x^2}{2} + x - \ln(1+x) + C_2$$

$$\boxed{-\frac{y^2}{2} - y - \ln(1-y) + \frac{x^2}{2} - x + \ln(1+x) = C_1}$$

$$\text{SolGral} := y + \frac{1}{2}y^2 + \ln(-1+y) - \frac{1}{2}x^2 + x - \ln(1+x) = C$$

$$\int \frac{y^2}{1-y} dy = \int \left(-y - 1 + \frac{1}{1-y} \right) dy = -\frac{y^2}{2} - y - \ln(1-y) + \frac{x^2}{2} - x + \ln(1+x) = C.$$

$$\frac{y^2}{1-y} = -y - 1 + \frac{1}{1-y}$$

$$\begin{array}{r} -y-1 \\ -y+1 \overline{) y^2} \\ \underline{-y^2+y} \\ 0 -y+1 \end{array}$$

$$3e^x \tan(y) + (2 - e^x) \sec^2(y) \frac{dy}{dx} = 0$$

$$\frac{3e^x}{2 - e^x} dx + \frac{\sec^2(y)}{\tan(y)} dy = 0 \quad \wedge$$

$$-3 \int \frac{-e^x}{(2 - e^x)} dx + \int \frac{\sec^2(y)}{\tan(y)} dy = 0$$

$$\int -3 \ln(2 - e^x) + \ln(\tan(y)) = C.$$

$$\ln(2 - e^x)^{-3} + \ln(\tan(y)) = C$$

$$\ln\left(\frac{1}{(2 - e^x)^3}\right) + \ln(\tan(y)) = C$$

$$\ln\left(\frac{\tan(y)}{(2 - e^x)^3}\right) = C$$

$$\frac{\tan(y)}{(2 - e^x)^3} = e^C$$

$$\tan(y) = C (2 - e^x)^3$$

$$y = \arctan\left(C (2 - e^x)^3\right)$$

$$\frac{dy}{dx} + \frac{y}{x} = 0$$

$$a_0(x) \frac{dy}{dx} + a_1(x) y = Q(x)$$

$$a_0(x) = 1$$

$$a_1(x) = \frac{1}{x} \quad \text{EDO (1)} L.$$

$$Q(x) = 0$$

$$\frac{dy}{dx} + \frac{y}{x} = 0$$

$$P(x) = \frac{1}{x}$$

$$\frac{dy}{y} + \frac{dx}{x} = 0$$

$$Q(y) = y$$

$$R(x) = 1$$

$$S(y) = 1$$

$$\int \frac{dy}{y} + \int \frac{dx}{x} = C$$

$$\int \frac{P(x)}{R(x)} dx + \int \frac{S(y)}{Q(y)} dy = C$$

$$L y + L x = C$$

$$L y x = C$$

$$y x = e^C$$

$$\boxed{y = \frac{C}{x}}$$