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> restart
> Ecua := (sin(x*y(x)) + x*y(x)*cos(x*y(x))) + (x*2*cos(x*y(x)))*diff(y(x), x)
      Ecua := sin(x y(x)) + x y(x) cos(x y(x)) + x^2 cos(x y(x)) (d/dx y(x))
(1)

> with(DEtools):
> odeadvisor(Ecua)
      [[_homogeneous, class G], _exact]
(2)

> M(x, y) := sin(x y) + x y cos(x y)
      M(x, y) := sin(x y) + x y cos(x y)
(3)

> N(x, y) := x^2 cos(x y)
      N(x, y) := x^2 cos(x y)
(4)

> ComprobacionUno := diff(M(x, y), y) = diff(N(x, y), x)
      ComprobacionUno := 2 cos(x y) x - x^2 y sin(x y) = 2 cos(x y) x - x^2 y sin(x y)
(5)

> ComprobacionDos := diff(M(x, y), y) - diff(N(x, y), x) = 0
      ComprobacionDos := 0 = 0
(6)

> IntMx := int(M(x, y), x)
      IntMx := -cos(x y)/y + (cos(x y) + sin(x y) x y)/y
(7)

> SolGral := simplify(IntMx + int((N(x, y) - diff(IntMx, y)), y)) = C
      SolGral := sin(x y) x = C
(8)

> IntNy := int(N(x, y), y)
      IntNy := sin(x y) x
(9)

> SolGralDos := simplify(IntNy + int((M(x, y) - diff(IntNy, x)), x)) = C
      SolGralDos := sin(x y) x = C
(10)

> exactsol(Ecua)
      {
      arcsin(-CI/x)
      y(x) = - ----
      x
      }
(11)

> restart
> Ecua := exp(y(x)) * (1 + x*2) * diff(y(x), x) - 2*x*(1 + exp(y(x))) = 0
      Ecua := e^{y(x)} (x^2 + 1) (d/dx y(x)) - 2 x (1 + e^{y(x)}) = 0
(12)

> with(DEtools);
[AreSimilar, Closure, DENormal, DEplot, DEplot3d, DEplot_polygon, DFactor,
DFactorLCLM, DFactorsols, Dchangevar, Desingularize, FunctionDecomposition, GCRD,
Gosper, Heunsols, Homomorphisms, IVPsol, IsHyperexponential, LCLM, MeijerGsols,
MultiplicativeDecomposition, ODEInvariants, PDEchangecoords, PolynomialNormalForm,
RationalCanonicalForm, ReduceHyperexp, RiemannPsols, Xchange, Xcommutator, Xgauge,
Zeilberger, abelsol, adjoint, autonomous, bernoullisol, buildsol, buildsym, canoni, caseplot,
casesplit, checkrank, chinisol, clairautsol, constcoeffsols, convertAlg, convertsys,

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dalembertsol, dcoeffs, de2diffop, dfieldplot, diff_table, diffop2de, dperiodic_sols, dpolyform, dsubs, eigenring, endomorphism_charpoly, equinv, eta_k, eulersols, exactsol, expsols, exterior_power, firint, firtest, formal_sol, gen_exp, generate_ic, genhomosol, gensys, hamilton_eqs, hypergeomsols, hyperode, indicialeq, infgen, initialdata, integrate_sols, intfactor, invariants, kovacicsols, leftdivision, liesol, line_int, linearsol, matrixDE, matrix_riccati, maxdimsystems, moser_reduce, muchange, mult, mutest, newton_polygon, normalG2, ode_int_y, ode_y1, odeadvisor, odepde, parametricsol, particularsol, phaseportrait, poincare, polysols, power_equivalent, rational_equivalent, ratsols, redode, reduceOrder, reduce_order, regular_parts, regularsp, remove_RootOf, riccati_system, riccatisol, rifread, rifsimp, rightdivision, rtaylor, separablesol, singularities, solve_group, super_reduce, symgen, symmetric_power, symmetric_product, symtest, transinv, translate, untranslate, varparam, zoom]

$$\begin{aligned} &> \text{odeadvisor}(Ecua) \\ & \qquad \qquad \qquad [_{\text{separable}}] \end{aligned} \tag{14}$$

$$\begin{aligned} &> \text{SolGral} := \text{separablesol}(Ecua) \\ & \qquad \qquad \qquad \text{SolGral} := \{y(x) = \ln(_CI x^2 + _CI - 1)\} \end{aligned} \tag{15}$$

$$\begin{aligned} &> Ecua \\ & \qquad \qquad \qquad e^{y(x)} (x^2 + 1) \left(\frac{d}{dx} y(x) \right) - 2x (1 + e^{y(x)}) = 0 \end{aligned} \tag{16}$$

$$\begin{aligned} &> P(x) := -2x \\ & \qquad \qquad \qquad P(x) := -2x \end{aligned} \tag{17}$$

$$\begin{aligned} &> Q(y) := 1 + e^y \\ & \qquad \qquad \qquad Q(y) := 1 + e^y \end{aligned} \tag{18}$$

$$\begin{aligned} &> R(x) := x^2 + 1 \\ & \qquad \qquad \qquad R(x) := x^2 + 1 \end{aligned} \tag{19}$$

$$\begin{aligned} &> S(y) := e^y \\ & \qquad \qquad \qquad S(y) := e^y \end{aligned} \tag{20}$$

$$\begin{aligned} &> \text{SolGralDos} := \text{simplify} \left(\exp \left(\text{int} \left(\frac{P(x)}{R(x)}, x \right) + \text{int} \left(\frac{S(y)}{Q(y)}, y \right) \right) \right) = C \\ & \qquad \qquad \qquad \text{SolGralDos} := \frac{1 + e^y}{x^2 + 1} = C \end{aligned} \tag{21}$$

> restart

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