

$$L \frac{d^2 q}{dt^2} + R \frac{dq}{dt} + \frac{q}{C} = E \cdot u(t-a)$$

$$u(t-a) = \begin{cases} 0 & ; t \leq a \\ 1 & ; t > a \end{cases}$$

$$L = 1 \text{ Henry} \quad q(0) = 0 \quad i(0) = 0$$

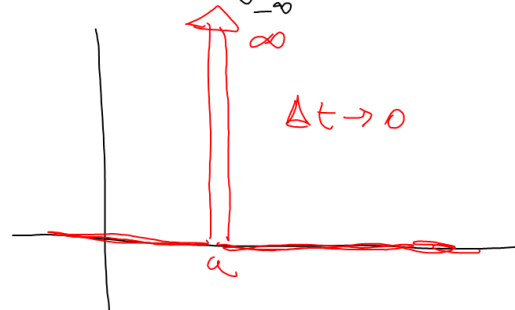
$$R = 20 \, \Omega$$

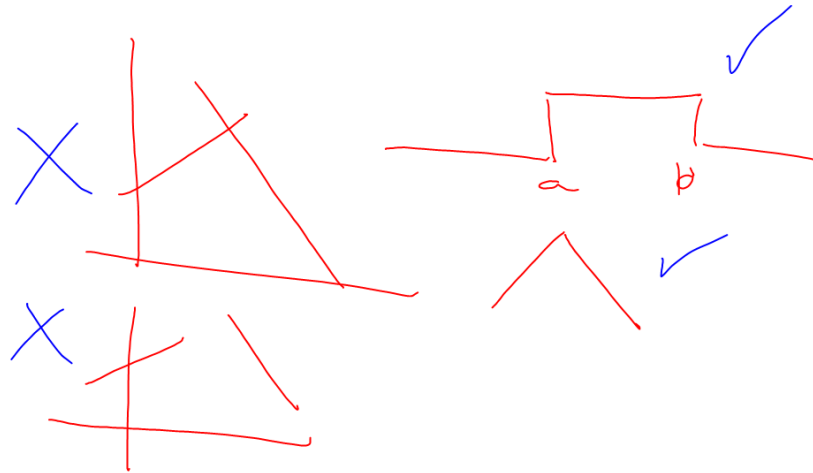
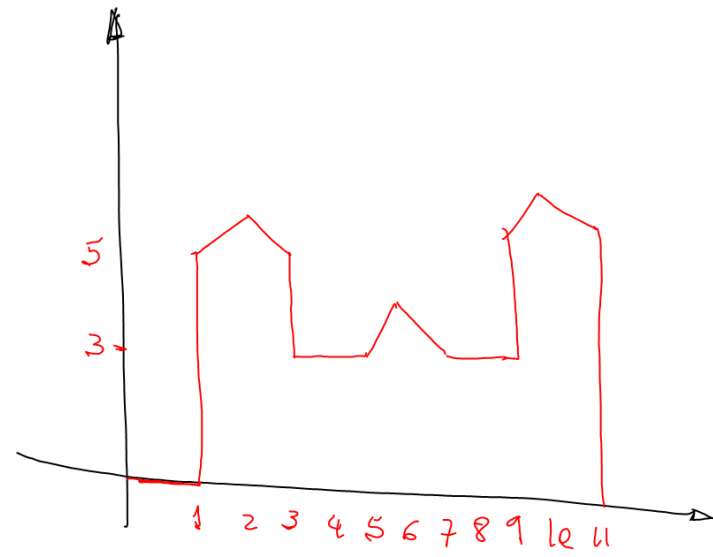
$$C = 0.005 \text{ faraday}$$

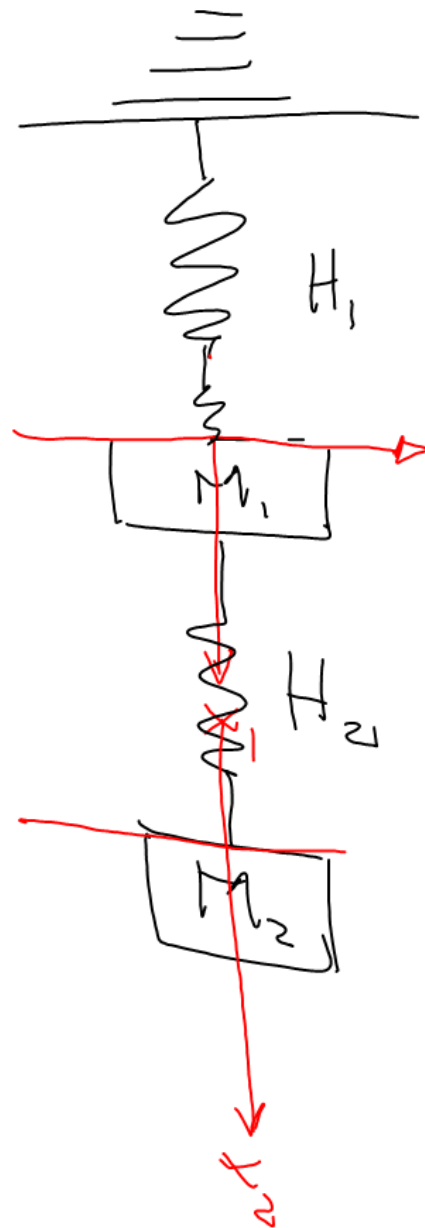
$$E = 150 \text{ V.}$$

$$i(t)$$

$$\delta(t-a) = \begin{cases} 0 & ; t \neq a \\ \int_{-\infty}^{\infty} \delta(t-a) dt = 1 & \end{cases} \quad \text{Dirac}$$







$$\sum F = M \frac{d^2 x}{dt^2}$$

$$-H_1 x_1 = M_1 \frac{d^2 x_1}{dt^2}$$

$$H_2(x_2 - x_1) - H_1 x_1 = M_1 \frac{d^2 x_1}{dt^2}$$

$$-H_2(x_2 - x_1) = M_2 \frac{d^2 x_2}{dt^2}$$

$$\begin{cases} \frac{dx}{dt} = a_{11}x + a_{12}y \\ \frac{dy}{dt} = a_{21}x + a_{22}y \end{cases}$$

↓
por sustitución

$$\frac{d^2 y}{dt^2} + b_1 \frac{dy}{dt} + b_2 y = 0$$

$$\frac{d}{dt} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} \quad \bar{X} = \begin{bmatrix} x \\ y \end{bmatrix} \quad A = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix}$$

$$\frac{d}{dt} \bar{X} = A \times \bar{X}$$

$$\frac{d^3 y}{dt^3} + b_1 \frac{d^2 y}{dt^2} + b_2 \frac{dy}{dt} + b_3 y = 0$$

$$y = y_1$$

$$\frac{dy}{dt} = \frac{dy_1}{dt} = y_2$$

$$\frac{d^2 y}{dt^2} = \frac{dy_2}{dt} = y_3$$

$$\frac{d^3 y}{dt^3} = \frac{dy_3}{dt}$$

$$\frac{dy_3}{dt} + b_1 y_3 + b_2 y_2 + b_3 y_1 = 0$$

$$\frac{dy_1}{dt} = y_2$$

$$\frac{dy_2}{dt} = y_3$$

$$\frac{dy_3}{dt} = -b_3 y_1 - b_2 y_2 - b_1 y_3$$

$$\frac{d}{dt} \begin{bmatrix} y_1 \\ y_2 \\ y_3 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -b_3 & -b_2 & -b_1 \end{bmatrix} \begin{bmatrix} y_1 \\ y_2 \\ y_3 \end{bmatrix}$$

$$\frac{d}{dt} \bar{y} = A_x \bar{y}$$

$$(m-1)(m-2)(m-3)=0$$

$$(m^2-3m+2)(m-3)=0$$

$$m^3-6m^2+11m-6=0$$

$$\frac{d}{dt} \bar{x} = A \times \bar{x} \quad \bar{x}(0)$$

$$\begin{bmatrix} e^{At} \end{bmatrix} \bar{x} = \begin{bmatrix} e^{At} \end{bmatrix} \cdot \bar{x}(0)$$

$$e^{at} \rightarrow \frac{de^{at}}{dt} = a e^{at}$$

$$e^{at} \Big|_{t=0} = 1$$

$$\frac{d}{dt} \begin{bmatrix} e^{At} \end{bmatrix} = A \begin{bmatrix} e^{At} \end{bmatrix}$$

$$\begin{bmatrix} e^{At} \end{bmatrix} \Big|_{t=0} = I.$$

$$\begin{bmatrix} e^{At} \end{bmatrix}^{-1} = e^{A(-t)}$$

$$\begin{bmatrix} e^{At} \end{bmatrix} \times \begin{bmatrix} e^{At} \end{bmatrix}^{-1} = I.$$