

$$\frac{\partial^2 z(x,y)}{\partial x^2} + \frac{\partial^2 z(x,y)}{\partial x \partial y} = z(x,y)$$

$$H_0 = z(x,y) = f(x) \cdot g(y)$$

$$\frac{\partial^2 z}{\partial x^2} = f'' \cdot g \quad \frac{\partial^2 z}{\partial x \partial y} = f' \cdot g'$$

$$f''g + f'g' = fg$$

$$f'g' = fg - f''g$$

$$\frac{g'}{g} = \frac{f-f''}{f'}$$

para $\alpha=0$

$$\frac{g'}{g} = 0 \quad \frac{f-f''}{f'} = 0$$

$$g'(y) = 0 \quad f-f'' = 0$$

$$g(y) = k, \quad f'' - f = 0$$

$$(D^2 - 1)f(x) = 0$$

$$(D+1)(D-1)f(x) = 0$$

$$f(x) = C_1 e^{-x} + C_2 e^x$$

$$z(x,y) = \underset{\alpha=0}{C_{10}} e^{-x} + C_{20} e^x$$

$$\frac{\partial z}{\partial x} = -C_{10} e^{-x} + C_{20} e^x \quad \frac{\partial z}{\partial y} = 0$$

$$\frac{\partial^2 z}{\partial x^2} = C_{10} e^{-x} + C_{20} e^x$$

$$(C_{10} e^{-x} + C_{20} e^x) + (0) = C_{10} e^{-x} + C_2 e^x$$

$\underbrace{0 \leq 0}$

$$\frac{\partial^2 z}{\partial x^2} + \frac{\partial^2 z}{\partial x \partial y} = 0$$

$$\alpha > 0 \quad \alpha = \beta^2 \quad \beta \neq 0$$

$$\frac{g'}{g} = \beta^2 \quad \frac{f-f''}{f'} = \beta^2$$

$$g' = \beta^2 g \quad f-f'' = \beta^2 f'$$

$$(D - \beta^2)g(y) = 0$$

$$g(y) = k_1 e^{\beta^2 y}$$

$$f'' + \beta^2 f' - f = 0$$

$$(D^2 + \beta^2 D - 1) f(x) = 0$$

$$m^2 + \beta^2 m - 1 = 0$$

$$m = \frac{-\beta^2 \pm \sqrt{\beta^4 + 4}}{2}$$

$$m_1 = \frac{-\beta^2 + \sqrt{\beta^4 + 4}}{2}$$

$$m_2 = \frac{-\beta^2 - \sqrt{\beta^4 + 4}}{2}$$

$$f(x) = C_1 e^{\left(\frac{-\beta^2 + \sqrt{\beta^4 + 4}}{2} x\right)} + C_2 e^{\left(\frac{-\beta^2 - \sqrt{\beta^4 + 4}}{2} x\right)}$$

$$z(x, y) = C e^{\beta y} \left(C_{10} e^{\left(\frac{-\beta^2 + \sqrt{\beta^4 + 4}}{2} x\right)} + C_{20} e^{\left(\frac{-\beta^2 - \sqrt{\beta^4 + 4}}{2} x\right)} \right)$$

$$\alpha < 0 \quad \alpha = -\beta^2$$

$$\frac{\zeta'}{\zeta} = -\beta^2 \quad \frac{F-F'}{F'} = -\beta^2$$

$$(\mathcal{D} + \beta^2) \zeta(y) = 0 \quad F - F' = -\beta^2 F'$$

$$\zeta(y) = C_1 e^{-\beta^2 y} \quad F' - \beta^2 F' - F = 0$$

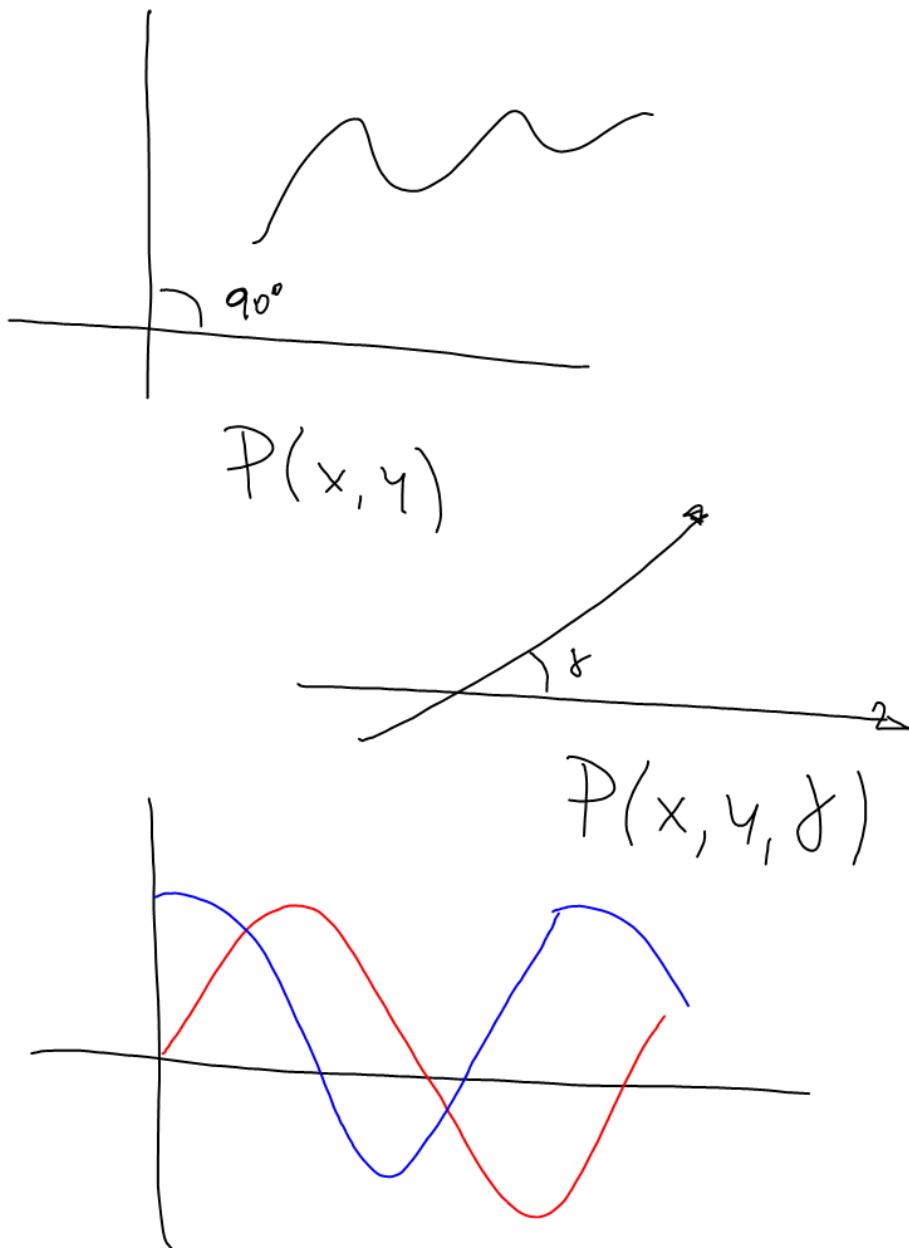
$$(\mathcal{D}^2 - \beta^2 - 1) F(x) = 0$$

$$\lambda^2 - \beta^2 - 1 = 0$$

$$\lambda = \frac{\beta^2 \pm \sqrt{\beta^4 + 1}}{2}$$

$$F(x) = C_1 e^{\left(\frac{\beta^2 + \sqrt{\beta^4 + 1}}{2}\right)x} + C_2 e^{\left(\frac{\beta^2 - \sqrt{\beta^4 + 1}}{2}\right)x}.$$

$$\begin{aligned} Z(x, y) &= e^{-\beta^2 y} \left(C_{10} e^{\left(\frac{\beta^2 + \sqrt{\beta^4 + 1}}{2}\right)x} + C_{20} e^{\left(\frac{\beta^2 - \sqrt{\beta^4 + 1}}{2}\right)x} \right) \\ &\text{for } \alpha < 0 \end{aligned}$$

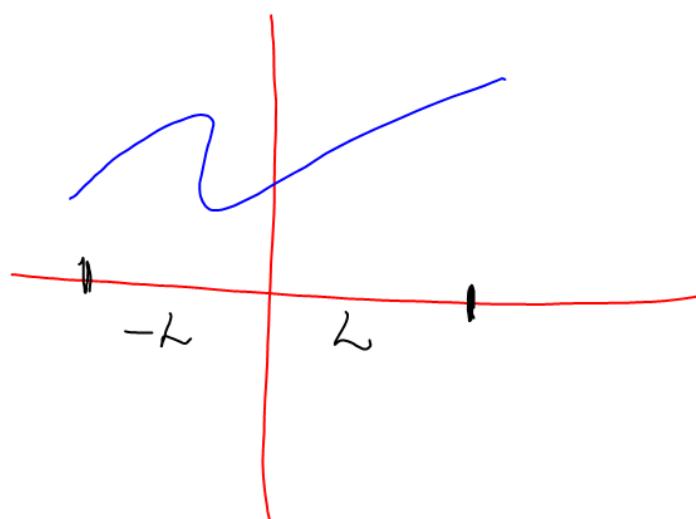


$$Z(x,y) = F_1(y + m_1 x) + F_2(y + m_2 x).$$



Serie Trigonométrica de Fourier

$$f(x) = C + \sum_{n=1}^{\infty} \left(a_n \cos\left(\frac{n\pi x}{L}\right) + b_n \operatorname{Sen}\left(\frac{n\pi x}{L}\right) \right).$$



$$C \quad a_0 \quad b_n$$

$$C = \frac{a_0}{2} \quad a_0 = \frac{1}{L} \int_{-L}^L f(x) dx.$$

$$a_n = \frac{1}{L} \int_{-L}^L f(x) \cos\left(\frac{n\pi x}{L}\right) dx$$

$$b_n = \frac{1}{L} \int_{-L}^L f(x) \sin\left(\frac{n\pi x}{L}\right) dx.$$

$$f(x) = x^2 - 3x \quad -2 \leq x \leq 2, \quad L=2$$

$$a_0 = \frac{1}{2} \int_{-2}^2 (x^2 - 3x) dx \Rightarrow \frac{1}{2} \left[\int x^2 dx \right]_{-2}^2 - \frac{3}{2} \left[\int x dx \right]_{-2}^2$$

$$= \frac{1}{2} \left[\frac{x^3}{3} \right]_{-2}^2 - \frac{3}{2} \left[\frac{x^2}{2} \right]_{-2}^2$$

$$= \frac{1}{2} \left(\frac{(2)^3}{3} - \frac{(-2)^3}{3} \right) - \frac{3}{2} \left(\frac{(2)^2}{2} - \frac{(-2)^2}{2} \right)$$

$$= \frac{1}{6}(16) \Rightarrow \frac{8}{3} \quad C = \frac{8}{6} \Rightarrow \frac{4}{3}$$

$$a_n = \frac{1}{2} \int_{-2}^2 (x^2 - 3x) \cos\left(\frac{n\pi x}{2}\right) dx$$

$$= \frac{1}{2} \left[\int x^2 \cos\left(\frac{n\pi x}{2}\right) dx - 3 \int x \cos\left(\frac{n\pi x}{2}\right) dx \right]_{-2}^2$$