

Clase 16-11-21

Tema IV - EDvnDP

$$F(x, y, z, \frac{\partial z}{\partial x}, \frac{\partial z}{\partial y}, \dots) = 0 \Rightarrow z(x, y) = f_1(x, y) + f_2(x, y) + \dots + f_n(x, y)$$

no conocemos  
su forma

Solución general

Condiciones  $\begin{cases} \text{iniciales} \\ \text{frontera} \end{cases}$

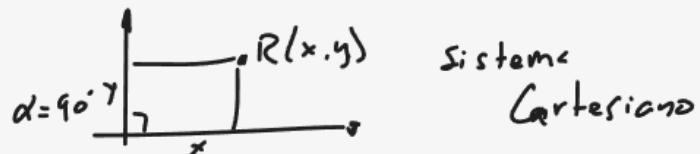
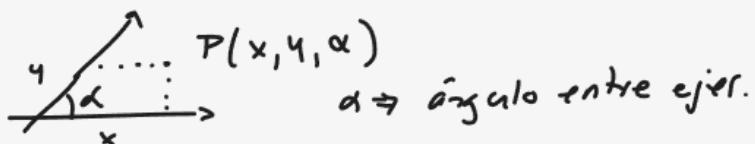
o ambas

puede  
no ser  
única

$z_{\text{particular}}$

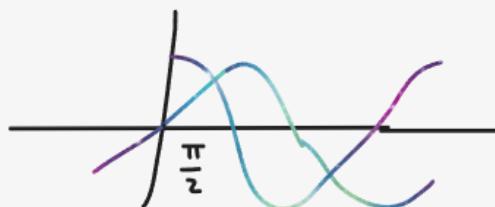
Los matemáticos siglo XIX

\* SERIE TRIGONOMÉTRICA FOURIER

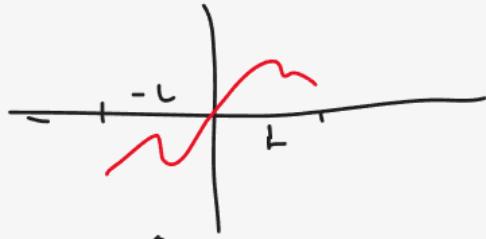


dos funciones que tengan propiedad  
carteriana entre sí, podremos  
representar cualquier función  $f(t)$   
en términos de ellas.

$$\sin(bt) \quad y \quad \cos(bt)$$



$$f(t) = F(\cos(bt), \sin(bt))$$



$-L \leq t < L$

$$f(t) = C + \sum_{n=1}^{\infty} \left( a_n \cos\left(\frac{n\pi}{L}t\right) + b_n \sin\left(\frac{n\pi}{L}t\right) \right)$$

$$C = \frac{a_0}{2} \quad a_0 = \frac{1}{L} \int_{-L}^L f(t) dt$$

$$a_n = \frac{1}{L} \int_{-L}^L f(t) \cos\left(\frac{n\pi}{L}t\right) dt$$

$$b_n = \frac{1}{L} \int_{-L}^L f(t) \sin\left(\frac{n\pi}{L}t\right) dt$$

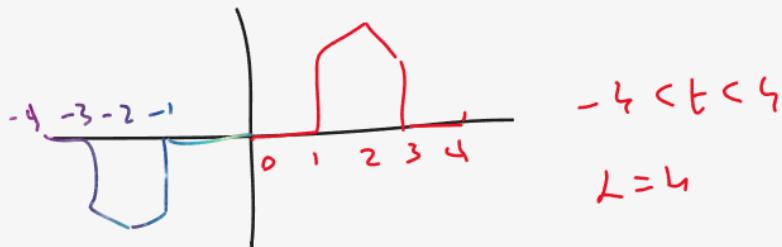
SERIE  
TRIGONOMÉTRICA  
DE FOURIER

una función es impar  $f(t)$

$$f(-t) = -f(t) \quad \left. \begin{array}{l} t \\ \end{array} \right\} \quad \begin{array}{l} a_0 = 0 \\ a_n = 0 \\ b_n \neq 0 \end{array}$$

una función es par  $f(t)$

$$f(-t) = f(t) \quad \left. \begin{array}{l} t^2 \\ \end{array} \right\} \quad \begin{array}{l} a_0 \neq 0 \\ a_n \neq 0 \\ b_n = 0 \end{array}$$



$-L < t < L$   
 $L = 4$