

> restart

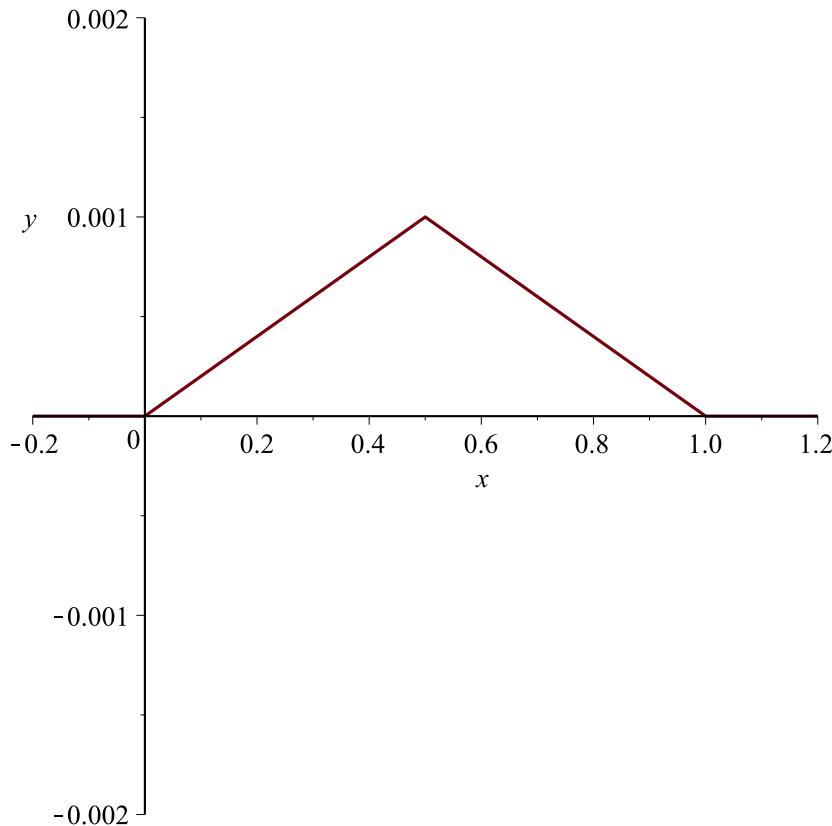
> Ecuacion := diff(y(x, t), t\$2) = c<sup>2</sup>·diff(y(x, t), x\$2)

$$Ecuacion := \frac{\partial^2}{\partial t^2} y(x, t) = c^2 \left( \frac{\partial^2}{\partial x^2} y(x, t) \right) \quad (1)$$

> CondFrontera := F(0) = 0, F(1) = 0

$$CondFrontera := F(0) = 0, F(1) = 0 \quad (2)$$

> CondIni := f = \left( \begin{array}{l} \frac{1}{1000} \cdot x \cdot \text{Heaviside}(x) - 2 \cdot \frac{1}{1000} \cdot \left( x - \frac{5}{10} \right) \cdot \text{Heaviside}\left( x - \frac{5}{10} \right) + \frac{1}{1000} \cdot (x - 1) \cdot \text{Heaviside}(x - 1) \\ \end{array} \right) : plot(rhs(CondIni), x = -0.2 .. 1.2, y = -0.002 .. 0.002)



> CondIniVel := fprima = 0

$$CondIniVel := fprima = 0 \quad (3)$$

> Ecuacion

$$\frac{\partial^2}{\partial t^2} y(x, t) = c^2 \left( \frac{\partial^2}{\partial x^2} y(x, t) \right) \quad (4)$$

> Hipotesis :=  $y(x, t) = F(x) \cdot G(t)$   
 $Hipotesis := y(x, t) = F(x) \cdot G(t)$  (5)

> EcuacionSeparable := eval(subs(y(x, t) = rhs(Hipotesis), Ecuacion))  
 $EcuacionSeparable := F(x) \left( \frac{d^2}{dt^2} G(t) \right) = c^2 \left( \frac{d^2}{dx^2} F(x) \right) G(t)$  (6)

> EcuacionSeparada := simplify( $\frac{lhs(EcuacionSeparable)}{F(x) \cdot G(t)}$ )  
 $= simplify\left(\frac{rhs(EcuacionSeparable)}{F(x) \cdot G(t)}\right)$   
 $EcuacionSeparada := \frac{\frac{d^2}{dt^2} G(t)}{G(t)} = \frac{c^2 \left( \frac{d^2}{dx^2} F(x) \right)}{F(x)}$  (7)

> EcuaX := rhs(EcuacionSeparada) = - $\beta^2$   
 $EcuaX := \frac{c^2 \left( \frac{d^2}{dx^2} F(x) \right)}{F(x)} = -\beta^2$  (8)

> EcuaT := lhs(EcuacionSeparada) = - $\beta^2$   
 $EcuaT := \frac{\frac{d^2}{dt^2} G(t)}{G(t)} = -\beta^2$  (9)

> c := 1  
 $c := 1$  (10)

> SolXneg := dsolve(EcuaX)  
 $SolXneg := F(x) = _C1 \sin(\beta x) + _C2 \cos(\beta x)$  (11)

> ParametroDos := simplify(subs(x = 0, rhs(SolXneg) = 0))  
 $ParametroDos := _C2 = 0$  (12)

> beta := n · Pi  
 $\beta := n \pi$  (13)

> SolXpart := subs(\_C2 = rhs(ParametroDos), SolXneg)  
 $SolXpart := F(x) = _C1 \sin(n \pi x)$  (14)

> SolTneg := dsolve(EcuaT)  
 $SolTneg := G(t) = _C1 \sin(n \pi t) + _C2 \cos(n \pi t)$  (15)

> SolUno := y(x, t) = subs(\_C1 = 1, rhs(SolXpart)) · rhs(SolTneg)  
 $SolUno := y(x, t) = \sin(n \pi x) (_C1 \sin(n \pi t) + _C2 \cos(n \pi t))$  (16)

> SolGeneral := y(x, t) = Sum(subs( $\underset{\infty}{\text{Sum}} \ C2 = b[n], _C1 = a[n], rhs(SolUno) ), n = 1 ..infinity)  
 $SolGeneral := y(x, t) = \sum_{n=1}^{\infty} \sin(n \pi x) (a_n \sin(n \pi t) + b_n \cos(n \pi t))$  (17)$

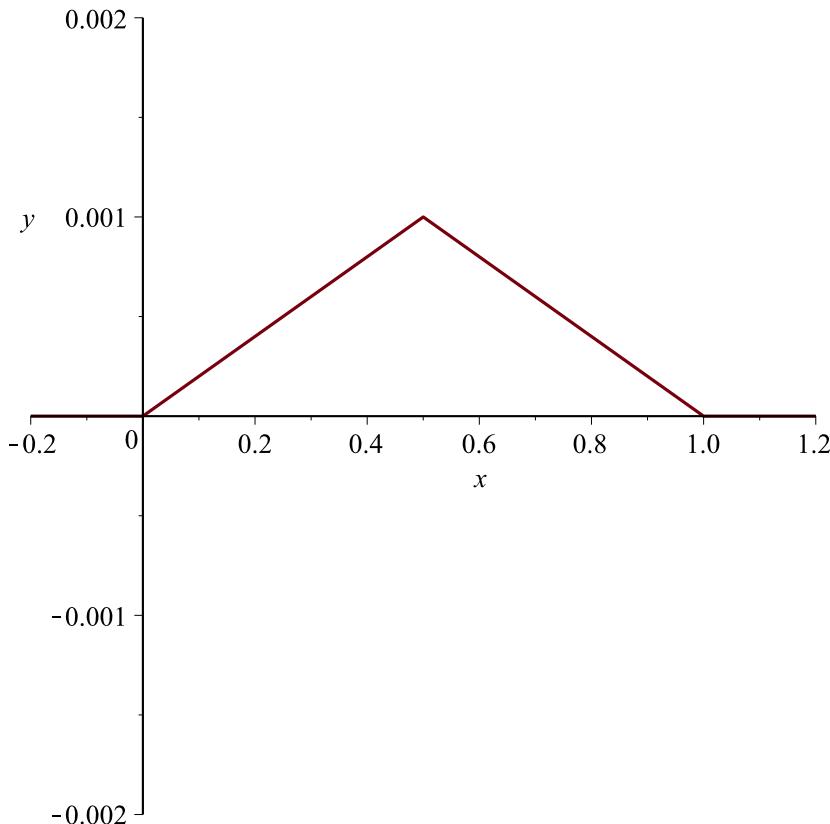
> SolPartIni := F(x) = eval(subs(t = 0, rhs(SolGeneral)))

$$SolPartIni := F(x) = \sum_{n=1}^{\infty} \sin(n\pi x) b_n \quad (18)$$

$$> L := \frac{5}{10}$$

$$L := \frac{1}{2} \quad (19)$$

>  $\text{plot}(\text{rhs}(CondIni), x = -0.2 .. 1.2, y = -0.002 .. 0.002)$



$$> b[n] := \left( \frac{1}{L} \right) \cdot \text{int}(\text{rhs}(CondIni) \cdot \sin(n\pi x), x = 0 .. 1)$$

$$b_n := \frac{1}{250} \frac{-\sin(n\pi) + 2 \sin\left(\frac{1}{2} n\pi\right)}{n^2 \pi^2} \quad (20)$$

$$> a[n] := 0$$

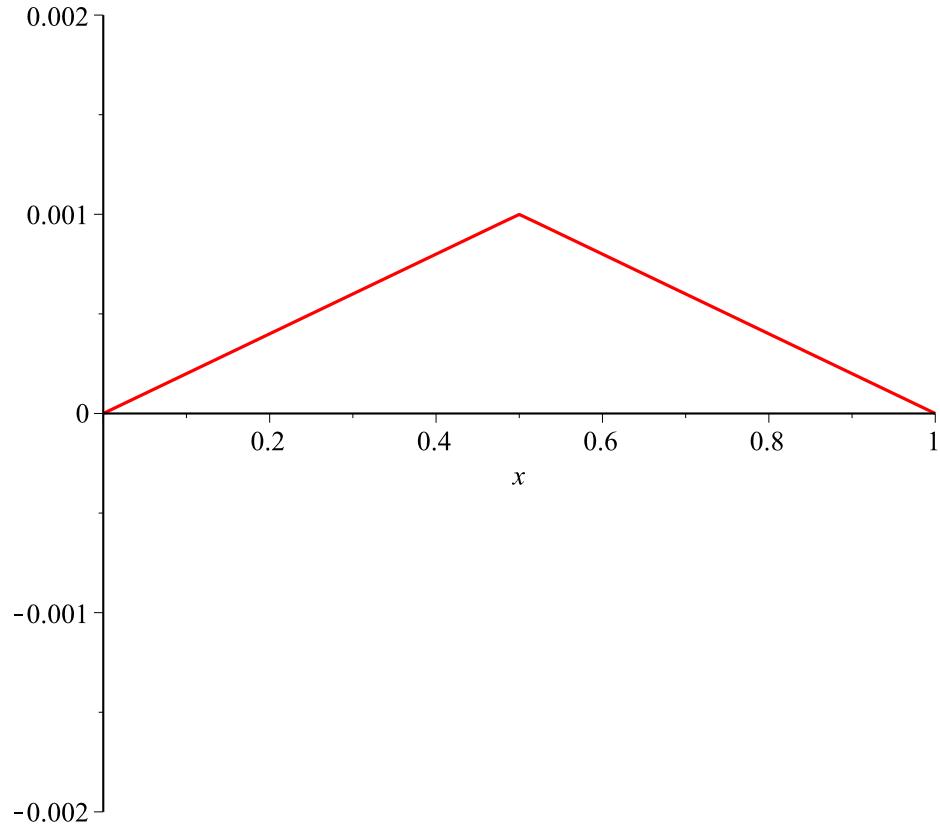
$$a_n := 0 \quad (21)$$

>  $SolParticular := y(x, t) = \text{Sum}(\text{subs}(_C2 = b[n], _CI = a[n], \text{rhs}(SolUno)), n = 1 .. 500) :$

>

>  $\text{with}(\text{plots}) :$

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> animate(rhs(SolParticular), x = 0 .. 1, t = 0 .. 4, frames = 150, view = [0 .. 1, -0.002 .. 0.002])
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[>
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