

> restart

> EcuacionDiferencial := $y' = \frac{y}{x}$

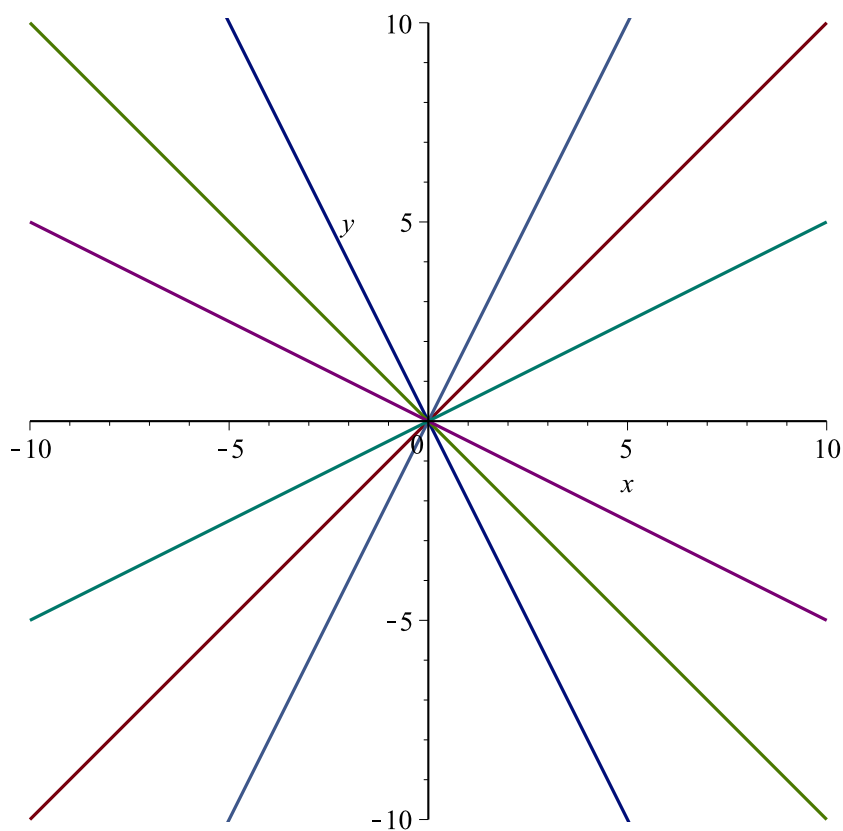
$$\text{EcuacionDiferencial} := \frac{d}{dx} y(x) = \frac{y(x)}{x} \quad (1)$$

> SolucionGeneral := dsolve(EcuacionDiferencial)

$$\text{SolucionGeneral} := y(x) = _C1 x \quad (2)$$

> ?scaling

> plot($\left\{ \text{subs}(_C1 = 1, \text{rhs}(\text{SolucionGeneral})), \text{subs}(_C1 = -1, \text{rhs}(\text{SolucionGeneral})), \text{subs}(_C1 = \frac{1}{2}, \text{rhs}(\text{SolucionGeneral})), \text{subs}(_C1 = -\frac{1}{2}, \text{rhs}(\text{SolucionGeneral})), \text{subs}(_C1 = 2, \text{rhs}(\text{SolucionGeneral})), \text{subs}(_C1 = -2, \text{rhs}(\text{SolucionGeneral})) \right\}$, $x = -10..10, y = -10..10$, $\text{scaling} = \text{constrained}$)



> restart

> Ecua := $(x^2 - y(x) \cdot x^2) + (y(x)^2 + x \cdot y(x)^2) \cdot \text{diff}(y(x), x) = 0$

$$Ecua := x^2 - y(x) x^2 + (y(x)^2 + x y(x)^2) \left(\frac{d}{dx} y(x) \right) = 0 \quad (3)$$

> with(DEtools) :

$$> odeadvisor(Ecua) \quad [_{separable}] \quad (4)$$

$$> M := factor(x^2 - y \cdot x^2) \quad M := -x^2 (y - 1) \quad (5)$$

$$> N := factor(y^2 + x \cdot y^2) \quad N := y^2 (x + 1) \quad (6)$$

$$> P := -x^2 \quad P := -x^2 \quad (7)$$

$$> Q := y - 1 \quad Q := y - 1 \quad (8)$$

$$> R := x + 1 \quad R := x + 1 \quad (9)$$

$$> S := y^2 \quad S := y^2 \quad (10)$$

$$> SolGral := int\left(\frac{P}{R}, x\right) + int\left(\frac{S}{Q}, y\right) = _{CI} \quad SolGral := -\frac{1}{2} x^2 + x - \ln(x + 1) + \frac{1}{2} y^2 + y + \ln(y - 1) = _{CI} \quad (11)$$

$$> Ecuacion := (4 \cdot x^2 + x \cdot y(x) - 3 \cdot y(x)^2) + (-5 \cdot x^2 + 2 \cdot x \cdot y(x) + y(x)^2) \cdot diff(y(x), x) = 0 \quad Ecuacion := 4 x^2 + x y(x) - 3 y(x)^2 + (-5 x^2 + 2 x y(x) + y(x)^2) \left(\frac{d}{dx} y(x) \right) = 0 \quad (12)$$

$$> odeadvisor(Ecuacion) \quad [_{homogeneous, class A}, _{rational}, _{dAlembert}] \quad (13)$$

$$> EcuaDos := factor(isolate(simplify(eval(subs(y(x) = x \cdot u(x), Ecuacion))), diff(u(x), x))) \quad EcuaDos := \frac{d}{dx} u(x) = -\frac{(u(x) - 1) (u(x) - 2) (u(x) + 2)}{x (u(x)^2 + 2 u(x) - 5)} \quad (14)$$

$$> odeadvisor(EcuaDos) \quad [_{separable}] \quad (15)$$

$$> P := \frac{1}{x} \quad P := \frac{1}{x} \quad (16)$$

$$> R := \frac{(u - 1) (u - 2) (u + 2)}{(u^2 + 2 u - 5)} \quad R := \frac{(u - 1) (u - 2) (u + 2)}{u^2 + 2 u - 5} \quad (17)$$

$$> SolDos := int(P, x) + int\left(\frac{1}{R}, u\right) = _{CI} \quad (18)$$

$$SolDos := \ln(x) + \frac{2}{3} \ln(u-1) - \frac{5}{12} \ln(u+2) + \frac{3}{4} \ln(u-2) = _CI \quad (18)$$

$$> SolDosMedio := expand(\exp(lhs(SolDos))) = _CI$$

$$SolDosMedio := \frac{x (u-1)^{2/3} (u-2)^{3/4}}{(u+2)^{5/12}} = _CI \quad (19)$$

$$> SolFinal := simplify\left(subs\left(u = \frac{y}{x}, lhs(SolDosMedio)\right)\right) = _CI$$

$$SolFinal := \frac{x \left(-\frac{-y+x}{x}\right)^{2/3} \left(-\frac{-y+2x}{x}\right)^{3/4}}{\left(\frac{y+2x}{x}\right)^{5/12}} = _CI \quad (20)$$

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