

CAPÍTULO I.- LA EDO(1).

EDO(1) NL

$$\text{C } M(x, y) + N(x, y) \frac{dy}{dx} = 0$$

$$\rightarrow F(x, y) = C,$$

(SG)

EDO (1) L CV $\left\{ \begin{array}{l} H \\ NH. \end{array} \right.$

$$\frac{dy}{dx} + p(x)y = q(x)$$

$$\text{Sg.} \Rightarrow y(x) = C_1 e^{-\int p(x) dx} + C_2 e^{\int p(x) dx} \int q(x) dx.$$

1- EDO(1) Lcv H.

$$\frac{dy}{dx} + p(x)y = 0$$

$$\frac{dy}{dx} = -p(x)y$$

$$\frac{dy}{y} = -p(x)dx$$

$$\int \frac{dy}{y} = - \int p(x)dx$$

$$Ly = - \int p(x)dx + LC_1$$

$$Ly - LC_1 = - \int p(x)dx$$

$$L\left(\frac{y}{C_1}\right) = - \int p(x)dx$$

$$\frac{y}{C_1} = e^{- \int p(x)dx}$$

$$\underline{SG_H} \quad y = C_1 e^{- \int p(x)dx}$$

$$\underline{EDO(1) Lcv H.} \quad \frac{dy}{dx} + p(x)y = 0$$

$$y(x) = C_1 e^{- \int p(x) dx}$$

$$y(x) = \frac{C_1}{e^{\int p(x) dx}}$$

$$e^{\int p(x) dx} y = C_1$$

$$f(x, y) = C_1$$

$$\frac{\partial F}{\partial x} + \frac{\partial F}{\partial y} \cdot \frac{dy}{dx} = 0$$

$$e^{\int p(x) dx} \cdot p(x) y + e^{\int p(x) dx} \cdot \frac{dy}{dx} = 0$$

$$e^{\int p(x) dx} \left(\frac{dy}{dx} + p(x) y \right) = 0$$

Factor

$$\text{Integrante. } e^{\int p(x) dx} \cdot y = C_1$$

$$\frac{dy}{dx} + p(x)y = q(x)$$

EDO(1) L'v NH.

$$e^{\int p(x)dx} \left(\frac{dy}{dx} + p(x)y \right) = e^{\int p(x)dx} q(x)$$

$$\frac{d}{dx} \left(e^{\int p(x)dx} \cdot y \right) = e^{\int p(x)dx} q(x)$$

$$\int d \left(e^{\int p(x)dx} \cdot y \right) = \int e^{\int p(x)dx} q(x) dx$$

$$e^{\int p(x)dx} \cdot y = \int e^{\int p(x)dx} q(x) dx + C_1$$

$$y = C e^{-\int p(x)dx} + e^{-\int p(x)dx} \int e^{\int p(x)dx} q(x) dx$$

EDO(1) L'v NH

$$\frac{dy}{dx} = \frac{1}{x \cos(y) + \sin(2y)} \quad y(x)$$

$$\frac{dx}{dy} = x \cos(y) + \sin(2y)$$

$$\frac{dx}{dy} - \cos(y) \cdot x = \sin(2y) \quad x(y)$$

$$P(y) = -\cos(y)$$

$$Q(y) = \sin(2y)$$

$$xLx \frac{dy}{dx} - y = x^3(3Lx - 1)$$

$$\frac{dy}{dx} - \frac{y}{xLx} = \frac{x^3(3Lx - 1)}{xLx}$$

$$= x^2(3Lx - 1)$$

$$-\frac{dy}{dx} - \frac{y}{xLx} = 3x^2 - \frac{x^2}{Lx}$$

$$\begin{aligned} p(x) &= -\frac{1}{xLx} \\ q(x) &= 3x^2 - \frac{x^2}{Lx} \end{aligned} \quad \left| \begin{array}{l} \int p(x) dx \\ - \int \frac{dx}{xLx} = - \int \frac{dx}{x} \end{array} \right.$$

$$\frac{\frac{a}{b}}{\frac{c}{d}} = \left(\frac{da}{cb} \right)$$

$$- \int \frac{dx}{x} = -L(Lx)$$

