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> restart
> Ecua := y' + 2·x·y = 2·x·exp(-x^2)
      Ecua :=  $\frac{d}{dx} y(x) + 2 x y(x) = 2 x e^{-x^2}$  (1)
> p := 2·x
      p := 2 x (2)
> q := rhs(Ecua)
      q := 2 x e^{-x^2} (3)
> IntPx := int(p, x)
      IntPx := x^2 (4)
> IntPositiva := exp(IntPx)
      IntPositiva := e^{x^2} (5)
> IntNegativa := exp(-IntPx)
      IntNegativa := e^{-x^2} (6)
> IntQx := int(IntPositiva·q, x)
      IntQx := x^2 (7)
> SolGral := y(x) = _C1·IntNegativa + IntNegativa·IntQx
      SolGral := y(x) = _C1 e^{-x^2} + x^2 e^{-x^2} (8)
> SolGraComp := dsolve(Ecua)
      SolGraComp := y(x) = (x^2 + _C1) e^{-x^2} (9)
> restart
> EcuaOriginal := diff(y(x), x) =  $\frac{1}{(x \cdot \cos(y(x)) + \sin(2 \cdot y(x)))}$ 
      EcuaOriginal :=  $\frac{d}{dx} y(x) = \frac{1}{x \cos(y(x)) + \sin(2 y(x))}$  (10)
> with(DEtools) :
> intfactor(EcuaOriginal)
       $\frac{\cos(y(x)) (2 \sin(y(x)) + x)}{x + 2 + 2 \sin(y(x))}$  (11)
> Ecuacion := diff(x(y), y) = x(y)·cos(y) + sin(2·y)
      Ecuacion :=  $\frac{d}{dy} x(y) = x(y) \cos(y) + \sin(2 y)$  (12)
> p := -cos(y)
      p := -cos(y) (13)
> q := sin(2 y)
      q := sin(2 y) (14)
> IntPos := int(p, y)
      IntPos := -sin(y) (15)
> IntNeg := -int(p, y)
      IntNeg := sin(y) (16)
> SolGral := x(y) = expand(_C1·exp(IntNeg) + exp(IntNeg)·int(exp(IntPos)·q, y))
      (17)

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$$\text{SolGral} := x(y) = _C1 e^{\sin(y)} - 2 \sin(y) - 2 \quad (17)$$

> Comprobar := dsolve(Ecuacion)

$$\text{Comprobar} := x(y) = _C1 e^{\sin(y)} - 2 \sin(y) - 2 \quad (18)$$

> restart

$$\text{Ecuacion} := \text{diff}(y(x), x) - \frac{y(x)}{x \cdot \log(x)} = 3 \cdot x^2 - \frac{x^2}{\log(x)}$$

$$\text{Ecuacion} := \frac{d}{dx} y(x) - \frac{y(x)}{x \ln(x)} = 3 x^2 - \frac{x^2}{\ln(x)} \quad (19)$$

$$p := -\frac{1}{x \cdot \log(x)}$$

$$p := -\frac{1}{x \ln(x)} \quad (20)$$

> q := rhs(Ecuacion)

$$q := 3 x^2 - \frac{x^2}{\ln(x)} \quad (21)$$

> IntNeg := -int(p, x)

$$\text{IntNeg} := \ln(\ln(x)) \quad (22)$$

> IntPos := int(p, x)

$$\text{IntPos} := -\ln(\ln(x)) \quad (23)$$

> SolGral := y(x) = _C1 \cdot \exp(IntNeg) + \exp(IntNeg) \cdot \text{int}(\exp(IntPos) \cdot q, x)

$$\text{SolGral} := y(x) = _C1 \ln(x) + x^3 \quad (24)$$

> comprobar := dsolve(Ecuacion)

$$\text{comprobar} := y(x) = _C1 \ln(x) + x^3 \quad (25)$$

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