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> restart
> Ecua := diff(x(t), t$2) - 7*diff(x(t), t) + 12*x(t) = cos(3*t) + t^2
      Ecua :=  $\frac{d^2}{dt^2} x(t) - 7 \left( \frac{d}{dt} x(t) \right) + 12 x(t) = \cos(3 t) + t^2$  (1)
=
> SolGral := dsolve(Ecua)
SolGral :=  $x(t) = e^{3t} \_C2 + e^{4t} \_C1 + \frac{1}{12} t^2 + \frac{1}{150} \cos(3 t) - \frac{7}{150} \sin(3 t) + \frac{7}{72} t + \frac{37}{864}$  (2)
=
> EcuaHom := lhs(Ecua) = 0
      EcuaHom :=  $\frac{d^2}{dt^2} x(t) - 7 \left( \frac{d}{dt} x(t) \right) + 12 x(t) = 0$  (3)
=
> Q := rhs(Ecua)
      Q :=  $\cos(3 t) + t^2$  (4)
=
> EcuaCarac := m^2 - 7*m + 12 = 0
      EcuaCarac :=  $m^2 - 7 m + 12 = 0$  (5)
=
> Raiz := solve(EcuaCarac)
      Raiz := 4, 3 (6)
=
> xx[1] := exp(Raiz[1]*t)
      xx1 :=  $e^{4t}$  (7)
=
> xx[2] := exp(Raiz[2]*t)
      xx2 :=  $e^{3t}$  (8)
=
> SolHom := x(t) = _C1*xx[1] + _C2*xx[2]
      SolHom :=  $x(t) = e^{4t} \_C1 + e^{3t} \_C2$  (9)
=
> SolNoHom := x(t) = AA*xx[1] + BB*xx[2]
      SolNoHom :=  $x(t) = AA e^{4t} + BB e^{3t}$  (10)
=
> with(linalg) :
> WW := wronskian([xx[1], xx[2]], t)
      WW :=  $\begin{bmatrix} e^{4t} & e^{3t} \\ 4 e^{4t} & 3 e^{3t} \end{bmatrix}$  (11)
=
> BB := array([0, Q])
      BB :=  $\begin{bmatrix} 0 & \cos(3 t) + t^2 \end{bmatrix}$  (12)
=
> Parametro := linsolve(WW, BB)
      Parametro :=  $\begin{bmatrix} \frac{\cos(3 t) + t^2}{e^{4t}} & -\frac{\cos(3 t) + t^2}{e^{3t}} \end{bmatrix}$  (13)
=
> Aprima := Parametro[1]; Bprima := Parametro[2]
      Aprima :=  $\frac{\cos(3 t) + t^2}{e^{4t}}$ 
      Bprima :=  $-\frac{\cos(3 t) + t^2}{e^{3t}}$  (14)

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$$\begin{aligned}
 &> AA := \text{simplify}(\text{int}(Aprima, t) + \_C1); BB := \text{simplify}(\text{int}(Bprima, t) + \_C2) \\
 AA &:= \frac{1}{800} (384 \sin(t) \cos(t)^2 - 512 \cos(t)^3 - 96 \sin(t) + 384 \cos(t) + 800 e^{4t} \_C1 - 200 t^2 \\
 &\quad - 100 t - 25) e^{-4t} \\
 BB &:= \frac{1}{54} (9 \cos(3 t) - 9 \sin(3 t) + 54 e^{3t} \_C2 + 18 t^2 + 12 t + 4) e^{-3t} \quad (15)
 \end{aligned}$$

$$\begin{aligned}
 &> SolFinal := \text{simplify}(SolNoHom) \\
 SolFinal &:= x(t) = \frac{12}{25} \sin(t) \cos(t)^2 - \frac{16}{25} \cos(t)^3 + e^{3t} \_C2 + \frac{1}{12} t^2 + e^{4t} \_C1 \\
 &\quad + \frac{1}{6} \cos(3 t) - \frac{3}{25} \sin(t) - \frac{1}{6} \sin(3 t) + \frac{7}{72} t + \frac{12}{25} \cos(t) + \frac{37}{864} \quad (16)
 \end{aligned}$$

$$\begin{aligned}
 &> SolGral \\
 x(t) &= e^{3t} \_C2 + e^{4t} \_C1 + \frac{1}{12} t^2 + \frac{1}{150} \cos(3 t) - \frac{7}{150} \sin(3 t) + \frac{7}{72} t + \frac{37}{864} \quad (17)
 \end{aligned}$$

$$\begin{aligned}
 &> Comprobar := \text{simplify}(\text{eval}(\text{subs}(x(t) = rhs(SolFinal), lhs(Ecua) - rhs(Ecua) = 0))) \\
 Comprobar &:= 0 = 0 \quad (18)
 \end{aligned}$$

$$\begin{aligned}
 &> ComprobarDos := \text{simplify}(\text{eval}(\text{subs}(x(t) = rhs(SolGral), lhs(Ecua) - rhs(Ecua) = 0))) \\
 ComprobarDos &:= 0 = 0 \quad (19)
 \end{aligned}$$

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