

> restart

> $Ecua := \text{diff}(u(x, y), x\$2) - 4 \cdot \text{diff}(u(x, y), x, y) + 4 \cdot \text{diff}(u(x, y), y\$2) = 0$

$$Ecua := \frac{\partial^2}{\partial x^2} u(x, y) - 4 \left(\frac{\partial^2}{\partial y \partial x} u(x, y) \right) + 4 \left(\frac{\partial^2}{\partial y^2} u(x, y) \right) = 0 \quad (1)$$

> $SolGralUno := u(x, y) = _F1(2 \cdot x + y) + x \cdot _F2(2 \cdot x + y)$

$$SolGralUno := u(x, y) = _F1(2 x + y) + x _F2(2 x + y) \quad (2)$$

> $SolGralDos := u(x, y) = _F1(2 \cdot x + y) + y \cdot _F2(2 \cdot x + y)$

$$SolGralDos := u(x, y) = _F1(2 x + y) + y _F2(2 x + y) \quad (3)$$

> $ComprobarUno := \text{simplify}(\text{eval}(\text{subs}(u(x, y) = \text{rhs}(SolGralUno), Ecua)))$

$$ComprobarUno := 0 = 0 \quad (4)$$

> $ComprobarDos := \text{simplify}(\text{eval}(\text{subs}(u(x, y) = \text{rhs}(SolGralDos), Ecua)))$

$$ComprobarDos := 0 = 0 \quad (5)$$

> $SolGralMaple := \text{pdsolve}(Ecua)$

$$SolGralMaple := u(x, y) = _F1(2 x + y) + x _F2(2 x + y) \quad (6)$$

> restart

> $Ecua := \text{diff}(u(x, t), t\$3) = 4 \cdot \text{diff}(u(x, t), t, x)$

$$Ecua := \frac{\partial^3}{\partial t^3} u(x, t) = 4 \left(\frac{\partial^2}{\partial x \partial t} u(x, t) \right) \quad (7)$$

> $EcuaDos := \text{eval}(\text{subs}(u(x, t) = F(x) \cdot G(t), Ecua))$

$$EcuaDos := F(x) \left(\frac{d^3}{dt^3} G(t) \right) = 4 \left(\frac{d}{dx} F(x) \right) \left(\frac{d}{dt} G(t) \right) \quad (8)$$

> $EcuaSep := \text{simplify}\left(\frac{\text{lhs}(EcuaDos)}{4 \cdot F(x) \cdot \text{diff}(G(t), t)}\right) = \text{simplify}\left(\frac{\text{rhs}(EcuaDos)}{4 \cdot F(x) \cdot \text{diff}(G(t), t)}\right)$

$$EcuaSep := \frac{1}{4} \frac{\frac{d^3}{dt^3} G(t)}{\frac{d}{dt} G(t)} = \frac{\frac{d}{dx} F(x)}{F(x)} \quad (9)$$

> $EcuaAlphaT := \text{lhs}(EcuaSep) = \text{alpha}$

$$EcuaAlphaT := \frac{1}{4} \frac{\frac{d^3}{dt^3} G(t)}{\frac{d}{dt} G(t)} = \alpha \quad (10)$$

> $EcuaAlphaX := \text{rhs}(EcuaSep) = \text{alpha}$

$$EcuaAlphaX := \frac{\frac{d}{dx} F(x)}{F(x)} = \alpha \quad (11)$$

> $EcuaCeroT := \text{subs}(\text{alpha} = 0, EcuaAlphaT)$

$$EcuaCeroT := \frac{1}{4} \frac{\frac{d^3}{dt^3} G(t)}{\frac{d}{dt} G(t)} = 0 \quad (12)$$

> $EcuaCeroX := \text{subs}(\text{alpha} = 0, EcuaAlphaX)$

$$EcuaCeroX := \frac{\frac{d}{dx} F(x)}{F(x)} = 0 \quad (13)$$

> SolCeroT := dsolve(EcuaCeroT)

$$SolCeroT := G(t) = \frac{1}{2} _C1 t^2 + _C2 t + _C3 \quad (14)$$

> SolCeroX := dsolve(EcuaCeroX)

$$SolCeroX := F(x) = _C1 \quad (15)$$

> SolGralCero := u(x, t) = subs(_C1 = 1, rhs(SolCeroX)) · rhs(SolCeroT)

$$SolGralCero := u(x, t) = \frac{1}{2} _C1 t^2 + _C2 t + _C3 \quad (16)$$

> EcuaPosT := subs(alpha = β², EcuaAlphaT)

$$EcuaPosT := \frac{1}{4} \frac{\frac{d^3}{dt^3} G(t)}{\frac{d}{dt} G(t)} = \beta^2 \quad (17)$$

> EcuaPosX := subs(alpha = β², EcuaAlphaX)

$$EcuaPosX := \frac{\frac{d}{dx} F(x)}{F(x)} = \beta^2 \quad (18)$$

> SolPosT := dsolve(EcuaPosT)

$$SolPosT := G(t) = _C1 + _C2 e^{2\beta t} + _C3 e^{-2\beta t} \quad (19)$$

> SolPosX := dsolve(EcuaPosX)

$$SolPosX := F(x) = _C1 e^{\beta^2 x} \quad (20)$$

> SolGralPos := u(x, t) = subs(_C1 = 1, rhs(SolPosX)) · rhs(SolPosT)

$$SolGralPos := u(x, t) = e^{\beta^2 x} (_C1 + _C2 e^{2\beta t} + _C3 e^{-2\beta t}) \quad (21)$$

> EcuaNegT := subs(alpha = -β², EcuaAlphaT)

$$EcuaNegT := \frac{1}{4} \frac{\frac{d^3}{dt^3} G(t)}{\frac{d}{dt} G(t)} = -\beta^2 \quad (22)$$

> EcuaNegX := subs(alpha = -β², EcuaAlphaX)

$$EcuaNegX := \frac{\frac{d}{dx} F(x)}{F(x)} = -\beta^2 \quad (23)$$

> SolNegT := dsolve(EcuaNegT)

$$SolNegT := G(t) = _C1 + _C2 \sin(2\beta t) + _C3 \cos(2\beta t) \quad (24)$$

> SolNegX := dsolve(EcuaNegX)

$$SolNegX := F(x) = _C1 e^{-\beta^2 x} \quad (25)$$

> SolGralNeg := u(x, t) = subs(_C1 = 1, rhs(SolNegX)) · rhs(SolNegT)

$$SolGralNeg := u(x, t) = e^{-\beta^2 x} (_C1 + _C2 \sin(2 \beta t) + _C3 \cos(2 \beta t)) \quad (26)$$

> Ecua

$$\frac{\partial^3}{\partial t^3} u(x, t) = 4 \left(\frac{\partial^2}{\partial x \partial t} u(x, t) \right) \quad (27)$$

> ComprobarCero := simplify(eval(subs(u(x, t) = rhs(SolGralCero), lhs(Ecua) - rhs(Ecua) = 0)))

$$ComprobarCero := 0 = 0 \quad (28)$$

> ComprobarPos := simplify(eval(subs(u(x, t) = rhs(SolGralPos), lhs(Ecua) - rhs(Ecua) = 0)))

$$ComprobarPos := 0 = 0 \quad (29)$$

> ComprobarNeg := simplify(eval(subs(u(x, t) = rhs(SolGralNeg), lhs(Ecua) - rhs(Ecua) = 0)))

$$ComprobarNeg := 0 = 0 \quad (30)$$