

Método del Operador Diferencial.

Edo(n)l.

$$\ddot{y} = -g \quad \left. \begin{array}{l} \frac{dy}{dx} \text{ Leibnitz.} \\ y' \\ \dot{y} \text{ Newton} \\ D_y \text{ O.D.} \end{array} \right\} \text{Derivada}$$

$$Dy \rightarrow \frac{dy}{dt} \rightarrow \frac{dy}{dx}$$

$$D(Dy) \Leftrightarrow D^2y$$

$$D(D^n y) \Leftrightarrow D^{n+1}y$$

$$D'(y) \rightarrow D(D'y) = y$$

$$\int y dx = D^{-1}y + C,$$

$$D^2y + a_1 Dy + a_2 y = 0$$

$$(D^2 + a_1 D + a_2)y = 0$$

$$m^2 + a_1 m + a_2 = 0 \quad \text{in } \mathbb{C}.$$

$$(m - a)(m - b) = 0$$

$$m_1 = a \quad m_2 = b$$

$$(D - a)(D - b)y = 0$$

$$y_g = c_1 e^{ax} + c_2 e^{bx}$$

$$(D - a)(D - b) \left[c_1 e^{ax} + c_2 e^{bx} \right] = 0$$

$$\frac{d^2 y}{dx^2} - 7 \frac{dy}{dx} + 12y = 0$$

$$D^2 y - 7Dy + 12y = 0$$

$$(D^2 - 7D + 12)y = 0$$

$$(D-4)(D-3)y = 0$$

$$y_g = c_1 e^{4x} + c_2 e^{3x}$$

$$(D-4)(D-3)[c_1 e^{4x} + c_2 e^{3x}] = 0$$

$$(D-4)[4c_1 e^{4x} + 3c_2 e^{3x} - 3c_1 e^{4x} - 3c_2 e^{3x}] = 0$$

$$(D-4)[c_1 e^{4x}] = 0$$

$$4c_1 e^{4x} - 4c_1 e^{4x} = 0$$

$$0 \equiv 0$$

$$(D-5)^2(D-4)y=0$$

$$(D^2-10D+25)(D-4)y=0$$

$$(D^3-10D^2+25D-4D^2+40D-100)y=0$$

$$(D^3-14D^2+65D-100)y=0$$

$$\left| \frac{d^3 y}{dx^3} - 14 \frac{d^2 y}{dx^2} + 65 \frac{dy}{dx} - 100y = 0 \right.$$

$$y_g = C_1 e^{5x} + C_2 x e^{5x} + C_3 e^{4x}$$

$$(D-5)^2(D-4)y=0$$

Case II Case I.

$$(D^2+4)(D+\sqrt{2})y=0$$

$$(D^3+\sqrt{2}D^2+4D+4\sqrt{2})y=0$$

$$y_g = C_1 \cos(2x) + C_2 \sin(2x) + C_3 e^{-\sqrt{2}x}$$

$$EDo(n) \subset \mathbb{C}[X] \text{ or } \mathbb{R}[X].$$

$$P(D)y = Q(x)$$

$$P(D)y = 0$$

$$y_{g/\mathbb{R}[X]} = y_{g/H} + y_{p/Q}.$$

$$\frac{d^2 y}{dx^2} - 4 \frac{dy}{dx} + 3y = 5e^{5x}$$

$$(D^2 - 4D + 3)y = 5e^{5x}$$

$$(D^2 - 4D + 3)y = 0$$

$$y_{g/\mathbb{R}[X]} = y_{g/H} + y_{p/Q}$$

$$(D-3)(D-1)y = 0$$

$$y_{g/H} = C_1 e^{3x} + C_2 e^x$$

NH

$$(D-3)(D-1)y = 5e^{5x}$$

$P(D)y$	$y(x)$
$(D-m)$	e^{mx}
$(D-m)^2$	$x e^{mx}$
$(D-m)^3$	$x^2 e^{mx}$
$(D-m)^{n+1}$	$x^n e^{mx}$
D	C_1
D^2	$C_1 x$
D^{n+1}	$C_1 x^n$
(D^2+b^2)	$\cos(bx)$ $\sin(bx)$
$(D^2+b^2)^2$	$x \cos(bx)$ $x \sin(bx)$
$(D^2+b^2)^{n+1}$	$x^n \cos(bx)$ $x^n \sin(bx)$

$((D-a)^2 + b^2)$	$e^{ax} \cos(bx)$ $e^{ax} \sin(bx)$
$((D-a)^2 + b^2)^2$	$x e^{ax} \cos(bx)$ $x e^{ax} \sin(bx)$
$((D-a)^2 + b^2)^{n+1}$	$x^n e^{ax} \cos(bx)$ $x^n e^{ax} \sin(bx)$

$$(D-3)(D-1)y = 5e^{5x} \text{ EDO(2) LCC H.}$$

$$(D-3)(D-1)(D-5)_A y = 0$$

$$y_g = C_1 e^{3x} + C_2 e^x + C_3 e^{5x} \text{ EDO(3) LCC H.}$$

$y_{g/H.}$

$y_{p/Q}$

$$y_g = C_1 e^{3x} + C_2 e^x + A e^{5x} \text{ COEFICIENTE INDETERMINADO}$$

$$y_{p/Q} = A e^{5x}$$

$$\frac{dy}{dx} = 5A e^{5x}$$

$$\frac{d^2 y}{dx^2} = 25A e^{5x}$$

$$\frac{d^2 y}{dx^2} - 4 \frac{dy}{dx} + 3y = 5e^{5x}$$

$$(25Ae^{5x}) - 4(5Ae^{5x}) + 3(Ae^{5x}) = 5e^{5x}$$

$$(25A - 20A + 3A)e^{5x} = 5e^{5x}$$

$$8Ae^{5x} = 5e^{5x}$$

$$8A = 5$$

$$A = \frac{5}{8}$$

$$y_g = c_1 e^{3x} + c_2 e^x + \frac{5}{8} e^{5x}$$

$$y'' - 4y' + 3y = 5e^{5x}$$

$$\frac{d^2 y}{dx^2} + 2 \frac{dy}{dx} + 2y = 2e^x + x^2 + \cos(2x)$$

$$(D^2 + 2D + 2)y = 0$$

$$((D+1)^2 + (1)^2)y = 0$$

$$y_g = C_1 e^{-x} \cos(x) + C_2 e^{-x} \sin(x)$$

$$\text{EDO(2)} \quad \text{NH} \left((D+1)^2 + (1)^2 \right) y = 2e^x + x^2 + \cos(2x)$$

$$\text{EDO(8)} \quad \text{H.} \left((D+1)^2 + (1)^2 \right) (D-1) D^3 (D^2 + 4) y = 0$$

$$y_g = C_1 e^{-x} \cos(x) + C_2 e^{-x} \sin(x) + C_3 e^x + C_4 x^2 + C_5 x + C_6 + C_7 \cos(2x) + C_8 \sin(2x)$$

$$y_{p/q} = A e^x + B x^2 + D x + E + F \cos(2x) + G \sin(2x)$$